

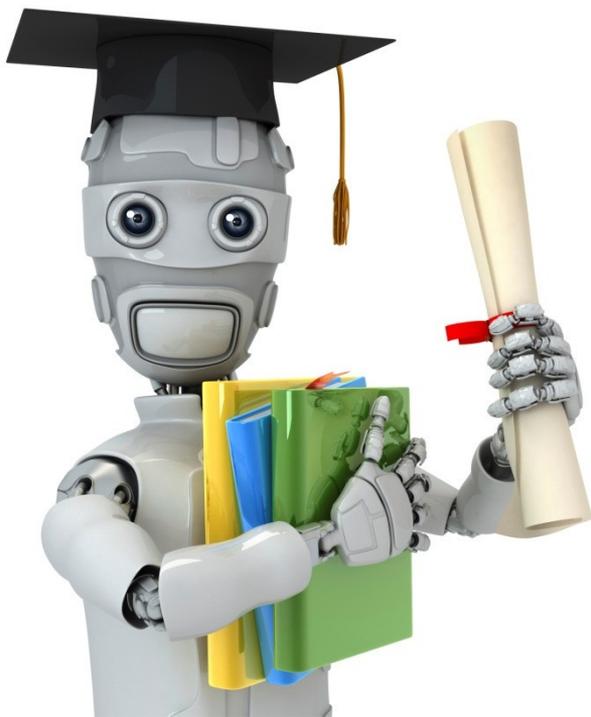
Machine Learning

Introduction

Welcome

Sachin Joshi –

Research Computing



Machine Learning

Contents

- Introduction
- Machine Learning Definition
- Supervised ML
- Unsupervised ML
- Linear Regression with one variable
 - Model Representation
 - Cost Function
 - Next Seminar – Gradient Descent Algorithm



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Machine Learning

- Grew out of work in AI
- New capability for computers

Examples:

- Database mining
 - Large datasets from growth of automation/web.
 - E.g., Web click data, medical records, biology, engineering
- Applications can't program by hand.
 - E.g., Autonomous helicopter, handwriting recognition, most of Natural Language Processing (NLP), Computer Vision.

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Examples:

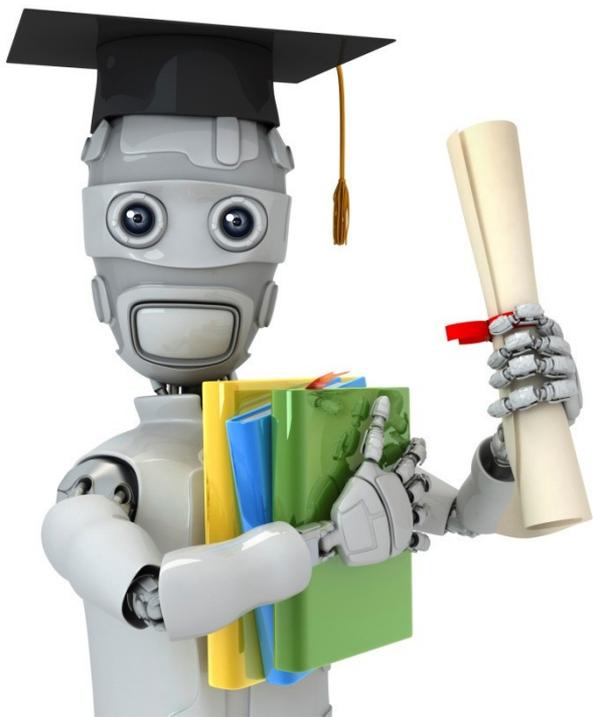
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- Applications can't program by hand.
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- Self-customizing programs
 - E.g., Amazon, Netflix product recommendations
- Understanding human learning (brain, real AI).



Machine Learning

Introduction

What is machine learning

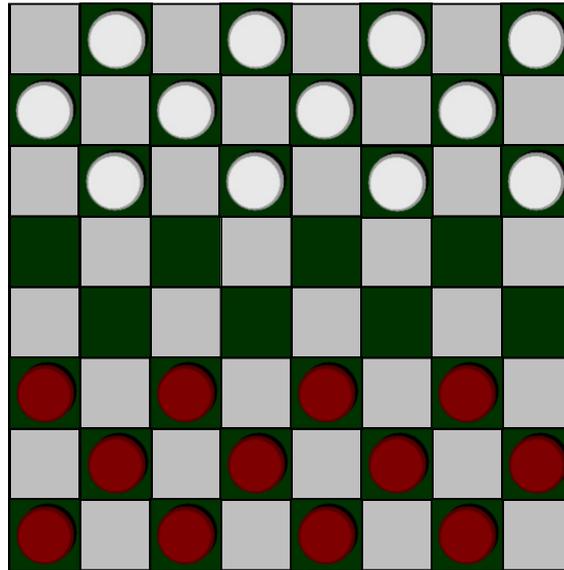
Machine Learning definition

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- Arthur Samuel (1959). Machine Learning: Field of study that gives computers the ability to learn without being explicitly programmed.

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Machine Learning definition

- Arthur Samuel (1959). Machine Learning: Field of study that gives computers the ability to learn without being explicitly programmed.
- Tom Mitchell (1998) Well-posed Learning Problem: A computer program is said to *learn* from experience E with respect to some task T and some performance measure P , if its performance on T , as measured by P , improves with experience E .

“A computer program is said to *learn* from experience E with respect to some task T and some performance measure P , if its performance on T , as measured by P , improves with experience E .”

Suppose your email program watches which emails you do or do not mark as spam, and based on that learns how to better filter spam. What is the task T in this setting?

- Classifying emails as spam or not spam.
- Watching you label emails as spam or not spam.
- The number (or fraction) of emails correctly classified as spam/not spam.
- None of the above—this is not a machine learning problem.

“A computer program is said to *learn* from experience E with respect to some task T and some performance measure P, if its performance on T, as measured by P, improves with experience E.”

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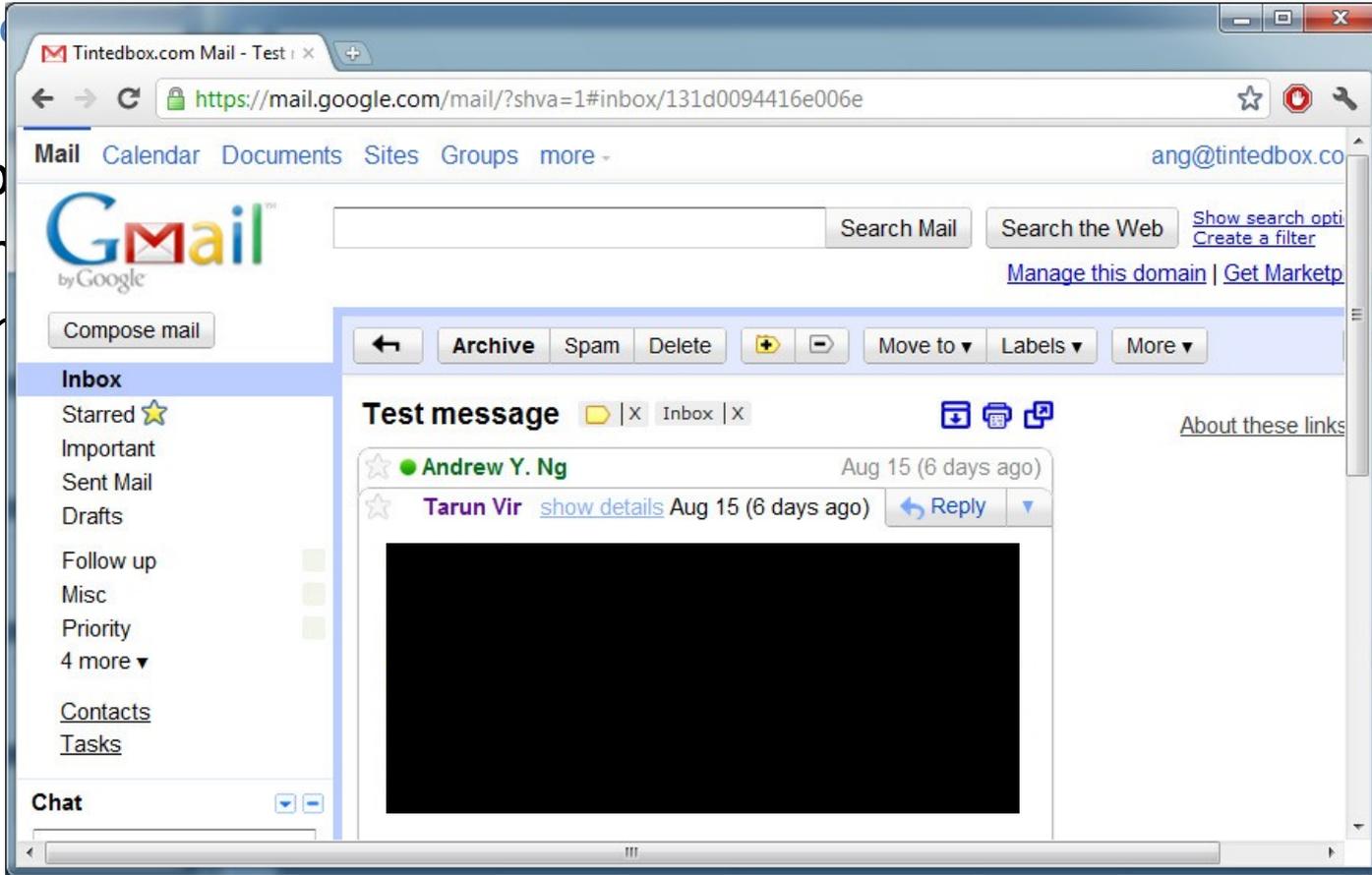
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Support on T,

Support not spam filter

Support
not spam
filter

Support
not spam
filter



Support
not spam.

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Machine learning algorithms:

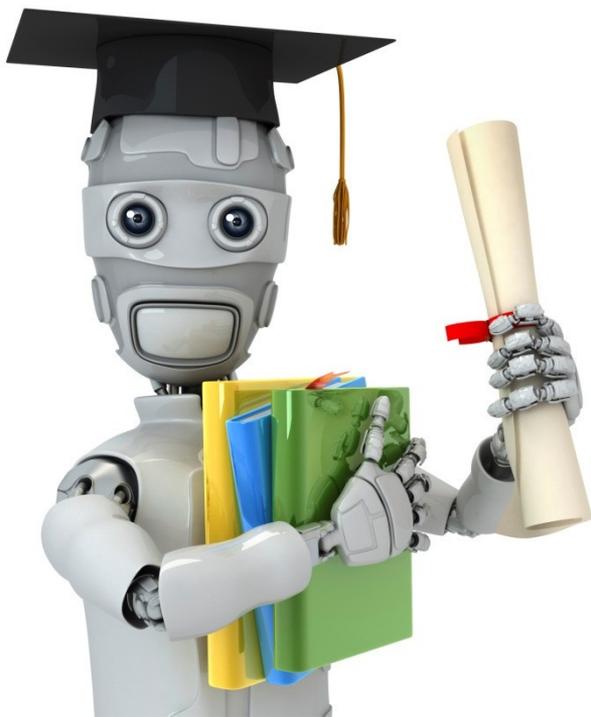
- Supervised learning
- Unsupervised learning



Others: Reinforcement learning, recommender systems.

Also talk about: Practical advice for applying learning algorithms.



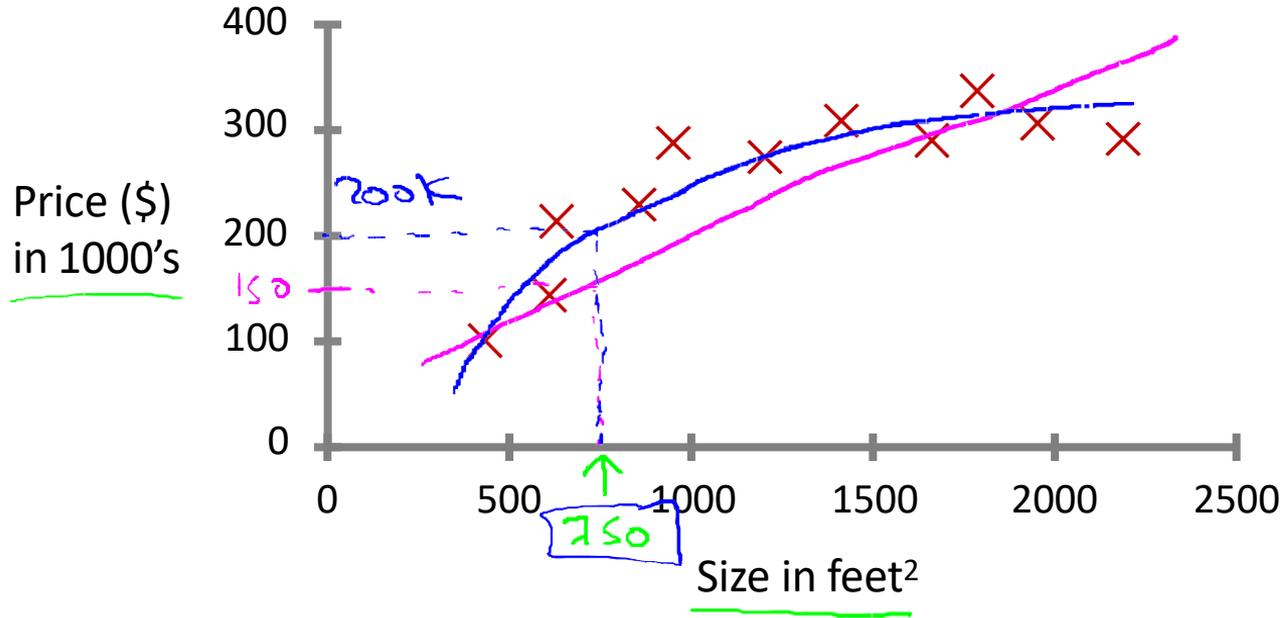


Machine Learning

Introduction

Supervised Learning

Housing price prediction.

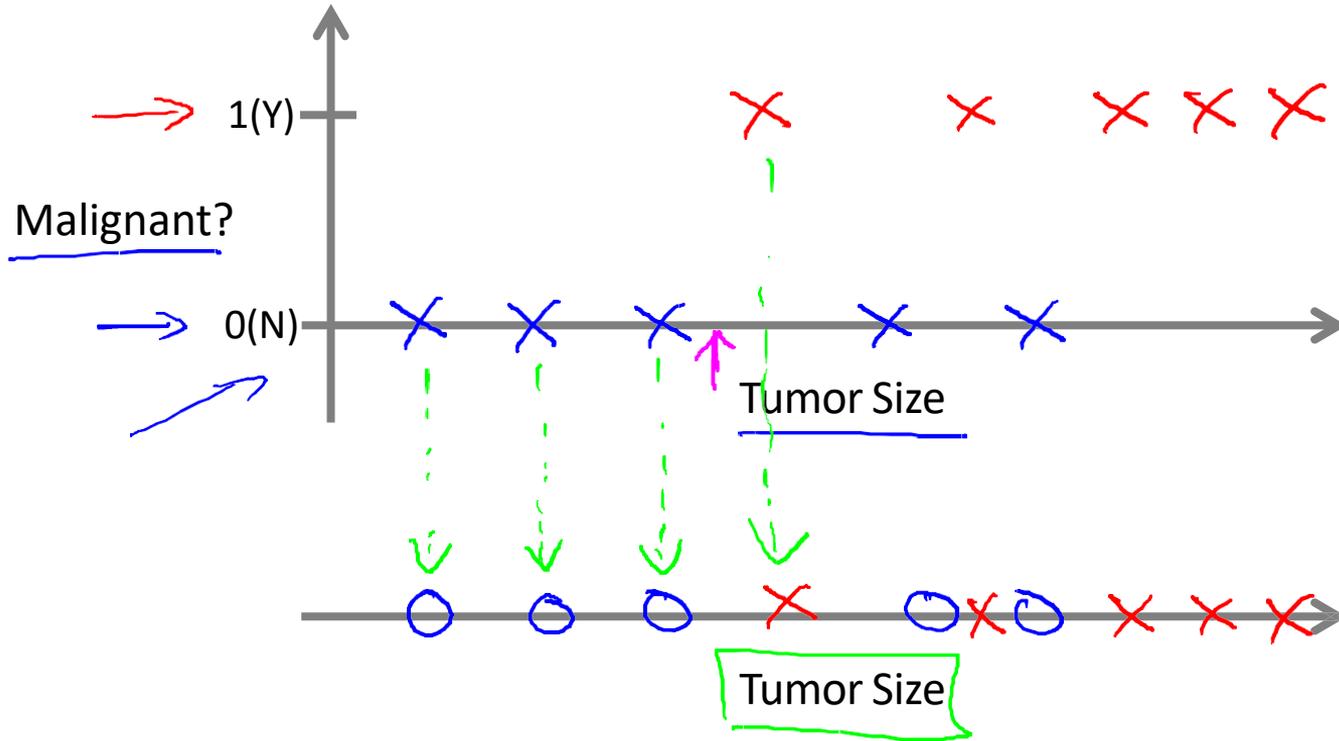


Supervised Learning

"right answers" given

Regression: Predict continuous valued output (price)

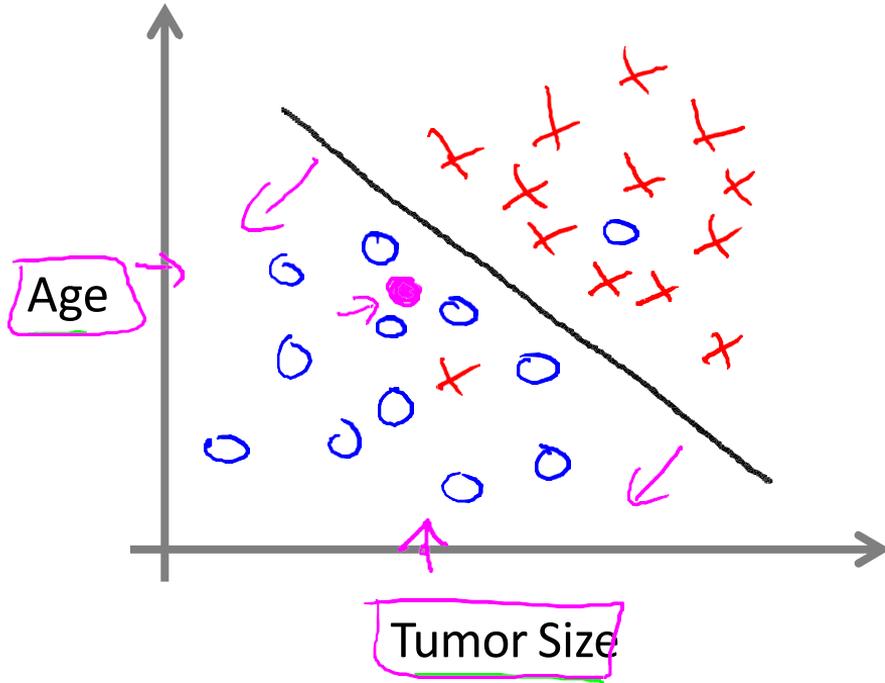
Breast cancer (malignant, benign)



Classification

Discrete valued
output (0 or 1)

0, 1, 2, 3
↓ benign type 1 cancer



- Clump Thickness
- Uniformity of Cell Size
- Uniformity of Cell Shape
- ...

You're running a company, and you want to develop learning algorithms to address each of two problems.

Problem 1: You have a large inventory of identical items. You want to predict how many of these items will sell over the next 3 months.

Problem 2: You'd like software to examine individual customer accounts, and for each account decide if it has been hacked/compromised.

Should you treat these as classification or as regression problems?

- Treat both as classification problems.
- Treat problem 1 as a classification problem, problem 2 as a regression problem.
- Treat problem 1 as a regression problem, problem 2 as a classification problem.
- Treat both as regression problems.

You're running a company, and you want to develop learning algorithms to address each of two problems.

1000's

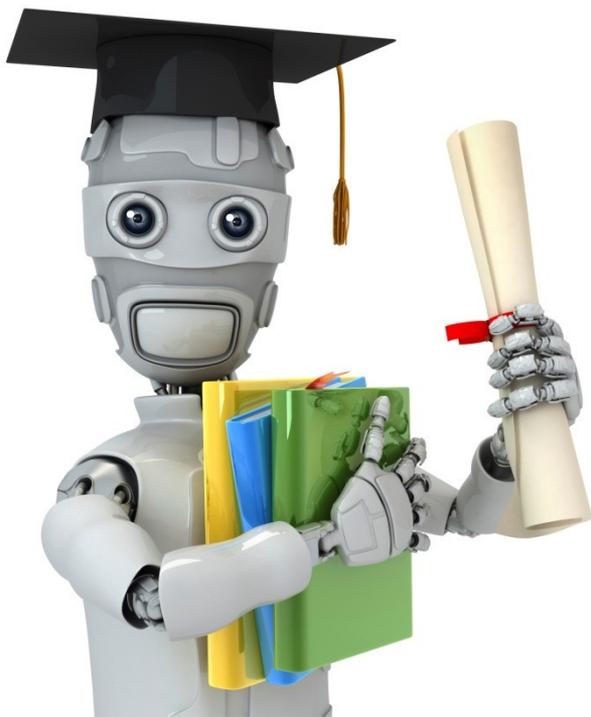
Problem 1: You have a large inventory of identical items. You want to predict how many of these items will sell over the next 3 months.

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0 - not hacked
1 - hacked

Should you treat these as classification or as regression problems?

- Treat both as classification problems.
- Treat problem 1 as a classification problem, problem 2 as a regression problem.
- Treat problem 1 as a regression problem, problem 2 as a classification problem.
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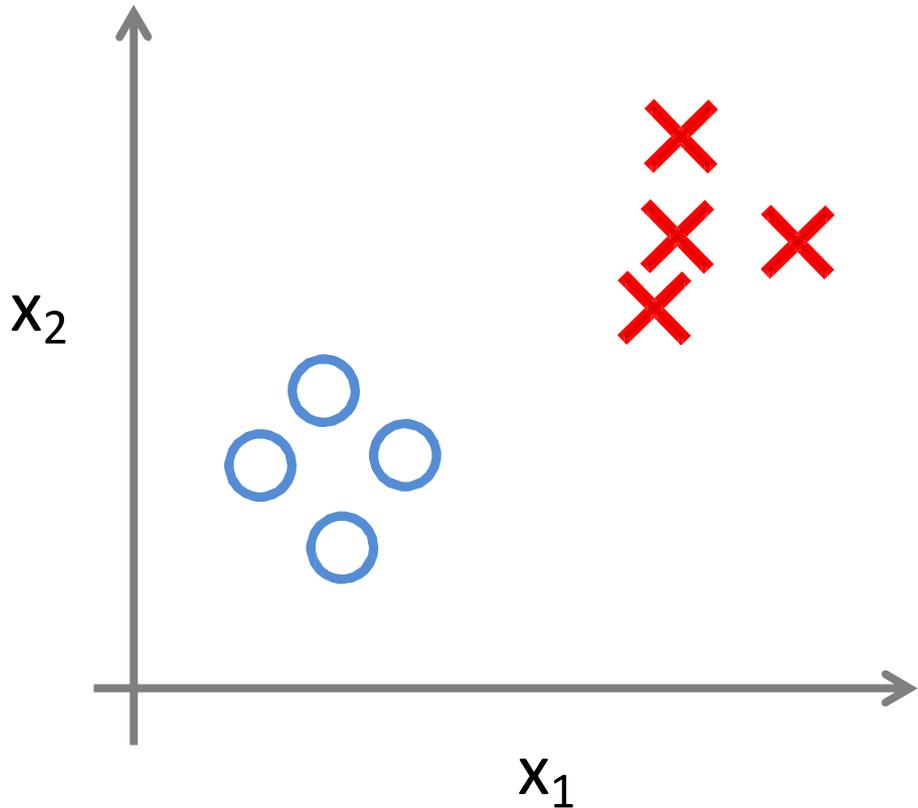


Machine Learning

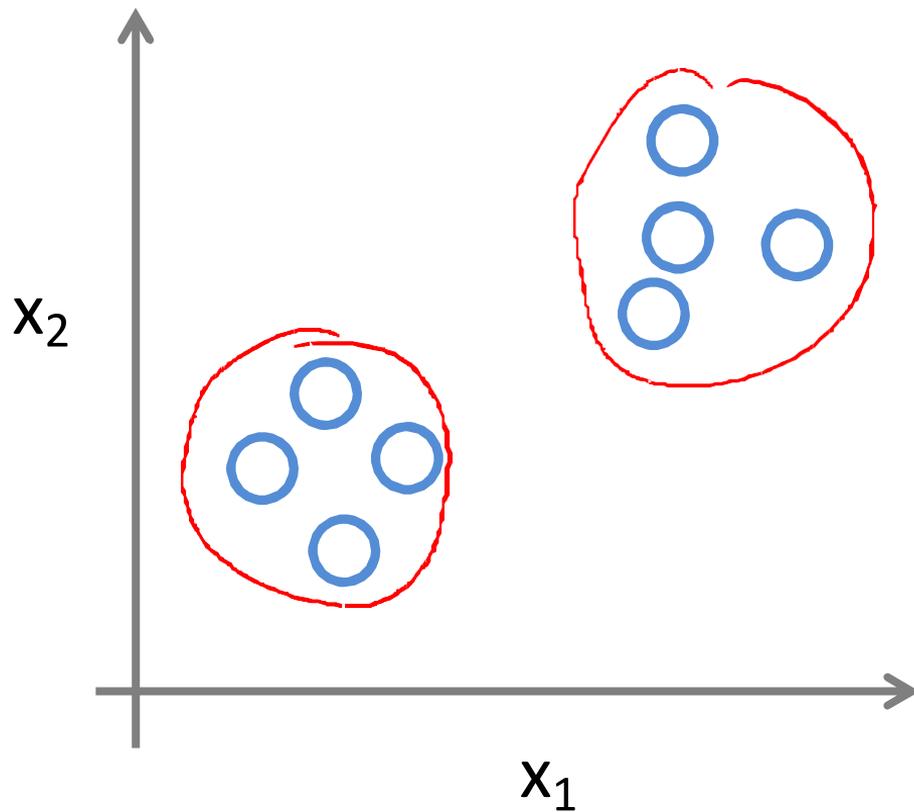
Introduction

Unsupervised Learning

Supervised Learning



Unsupervised Learning



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BP Oil Well, Site of National Catastrophe, Dies at One
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Spotlight

Sarkozy rages at EU 'humiliation'
 Financial Times - Peggy Hollinger - 2010

BP Kills Macondo, But Its Legacy Lives On

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SEPTEMBER 20, 2010 12:44 PM GMT

BP Kills Macondo, But Its Legacy Lives On

Article Comments (2)

By James Heron

BP confirmed late Sunday that the Macondo well that leaked almost five million barrels of oil into the Gulf of Mexico has been permanently sealed, but the well will continue to affect BP and the wider oil industry for many years.

The most immediate worry for BP and its shareholders is how the authorities will apportion blame for the spill. BP's own investigation cordoned responsibility across

Fire boat response crews battled the blazing remnants of the off shore oil rig Deepwater Horizon on April 21, 2010.

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Allien Well is dead, but much Gulf Coast work remains

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By The CNN Wire Staff

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STORY HIGHLIGHTS

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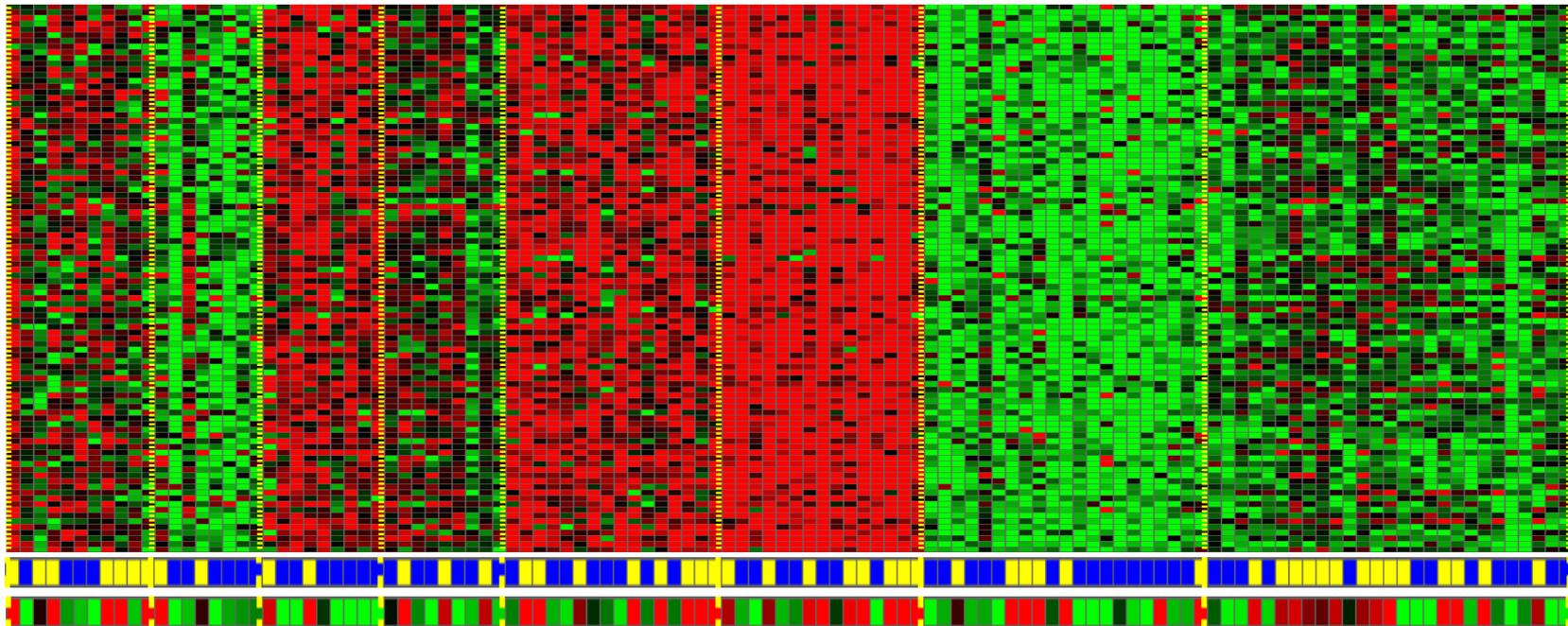
BP oil spill cost hits nearly \$10bn

BP has set up a \$20bn compensation fund after the Deepwater Horizon disaster, which has so far paid out 19,000 claims totalling more than \$240m

Julia Kollewe
 guardian.co.uk Monday 20 September 2010 08:33 BST
 article history

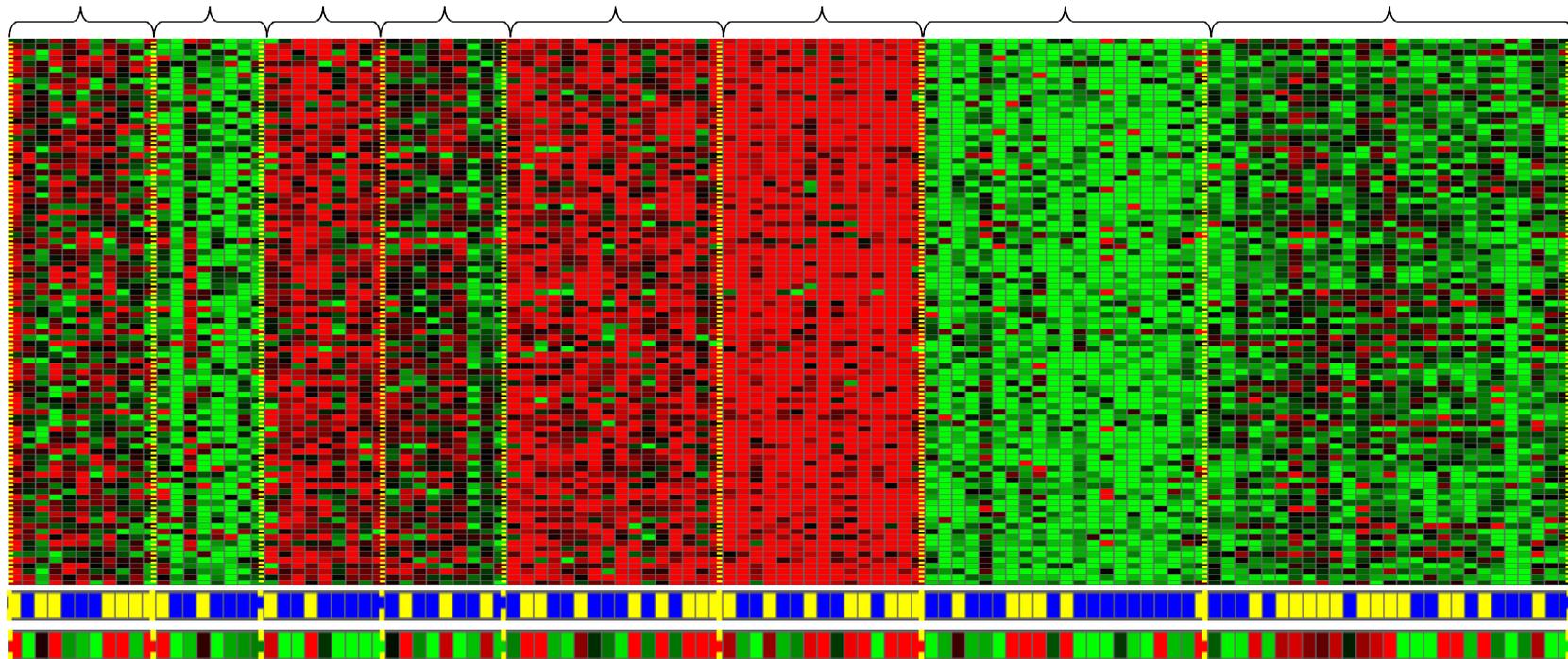
BP's costs for the Deepwater Horizon disaster have hit \$10bn. Photograph: HoReuters

Genes



Individuals

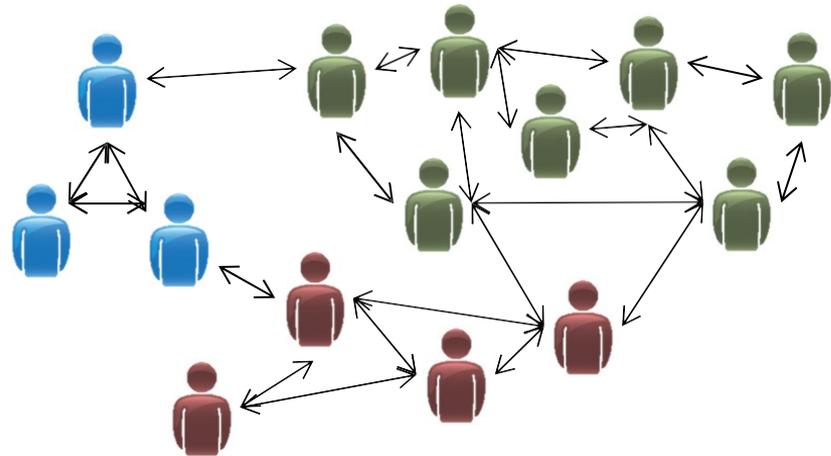
Genes



Individuals



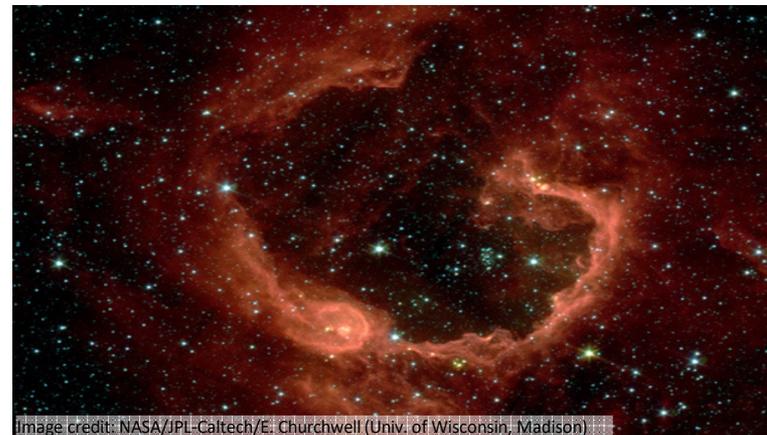
Organize computing clusters



Social network analysis

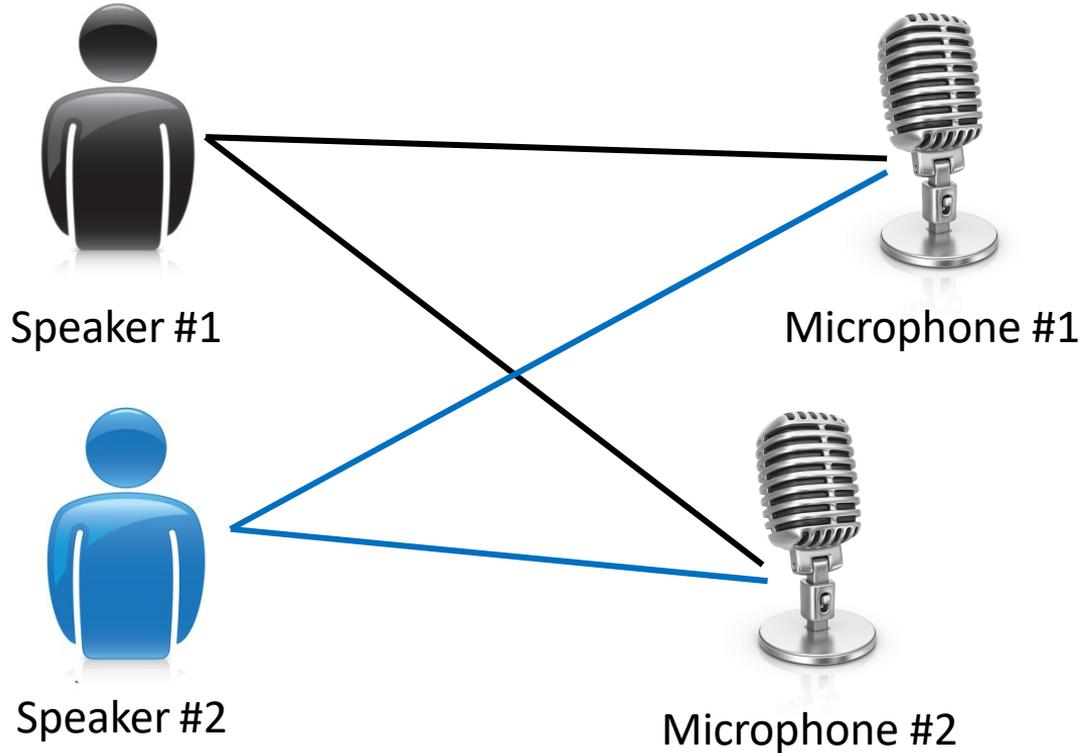


Market segmentation



Astronomical data analysis

Cocktail party problem



Cocktail party problem algorithm

```
[W,s,v] = svd(( repmat(sum(x.*x,1),size(x,1),1).*x)*x');
```

Of the following examples, which would you address using an unsupervised learning algorithm? (Check all that apply.)

- Given email labeled as spam/not spam, learn a spam filter.
- Given a set of news articles found on the web, group them into set of articles about the same story.
- Given a database of customer data, automatically discover market segments and group customers into different market segments.
- Given a dataset of patients diagnosed as either having diabetes or not, learn to classify new patients as having diabetes or not.

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Quiz 1 – ML Basics

1. A computer program is said to learn from experience E with respect to some Task T and some performance measure P if its performance on T, as measured by P, improves with experience E. Supposed we feed a learning algorithm a lot of historical weather data, and have it learn to predict weather. What would be a reasonable choice for P?

- The process of the algorithm examining a large amount of historical weather data.
- The weather prediction task.
- The probability of it correctly predicting a future date's weather.
- None of these.

2. Suppose you are working on weather prediction, and use a learning algorithm to predict tomorrow's temperature (in degrees Centigrade/Fahrenheit). Would you treat this as a classification or a regression problem?

- Regression
- Classification

3. Suppose you are working on stock market prediction, and you would like to predict the price of a particular stock tomorrow (measured in dollars). You want to use a learning algorithm for this. Would you treat this as a classification or a regression problem?

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4. Some of the problems below are best addressed using a supervised learning algorithm, and the others with an unsupervised learning algorithm. Which of the following would you apply supervised learning to? (Select all that apply.) In each case, assume some appropriate dataset is available for your algorithm to learn from.

- Take a collection of 1000 essays written on the US Economy, and find a way to automatically group these essays into a small number of groups of essays that are somehow "similar" or "related".
- Examine a large collection of emails that are known to be spam email, to discover if there are sub-types of spam mail.
- Given 50 articles written by male authors, and 50 articles written by female authors, learn to predict the gender of a new manuscript's author (when the identity of this author is unknown).
- Given historical data of children's ages and heights, predict children's height as a function of their age.

5. Which of these is a reasonable definition of machine learning?

- Machine learning is the field of allowing robots to act intelligently.
- Machine learning is the science of programming computers.
- Machine learning learns from labeled data.
- Machine learning is the field of study that gives computers the ability to learn without being explicitly programmed.

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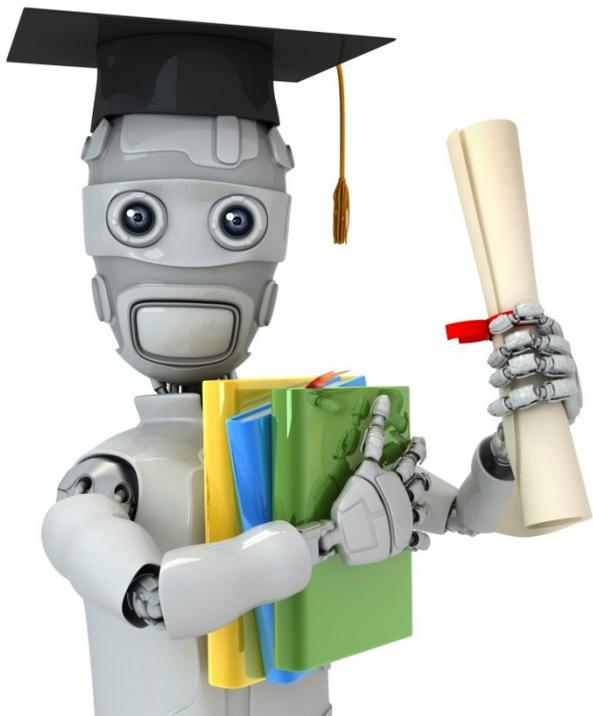
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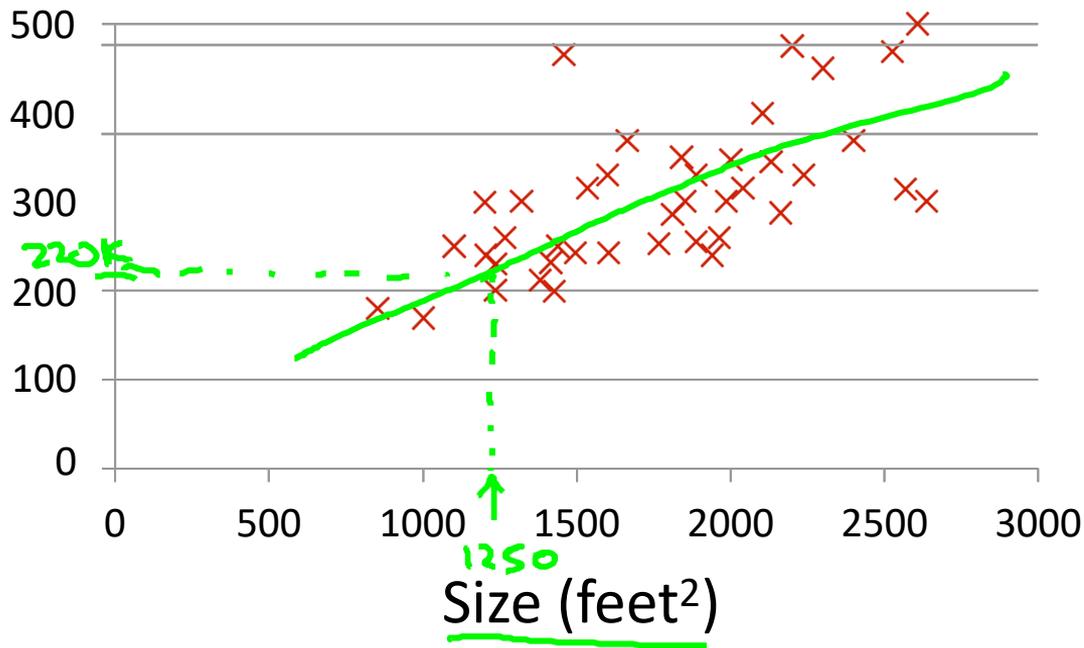
Machine Learning

Linear regression
with one variable

Model
representation

Housing Prices (Portland, OR)

Price
(in 1000s
of dollars)



Supervised Learning

Given the “right answer” for each example in the data.

Regression Problem

Predict real-valued output

Classification: Discrete-valued output

Training set of housing prices (Portland, OR)

Size in feet ² (x)	Price (\$) in 1000's (y)
→ 2104	460
1416	232
→ 1534	315
852	178
...	...

$m = 47$

Notation:

- m = Number of training examples
- x 's = "input" variable / features
- y 's = "output" variable / "target" variable

(x, y) - one training example
 $(x^{(i)}, y^{(i)})$ - i^{th} training example

$x^{(1)} = 2104$
 $x^{(2)} = 1416$
 $y^{(1)} = 460$

Consider the training set shown below. $(x^{(i)}, y^{(i)})$ is the i^{th} training example. What is $y^{(3)}$?

Size in feet ² (x)	Price(\$)
2104	460
1416	232
1534	315
852	178
....

- 1416
- 1534
- 315
- 0

Consider the training set shown below. $(x^{(i)}, y^{(i)})$ is the i^{th} training example. What is $y^{(3)}$?

Size in feet ² (x)	Price(\$)
2104	460
1416	232
1534	315
852	178
....

- 1416
- 1534
- 315
- 0

Training Set

Learning Algorithm

Size of house

h

Estimated price

hypothesis

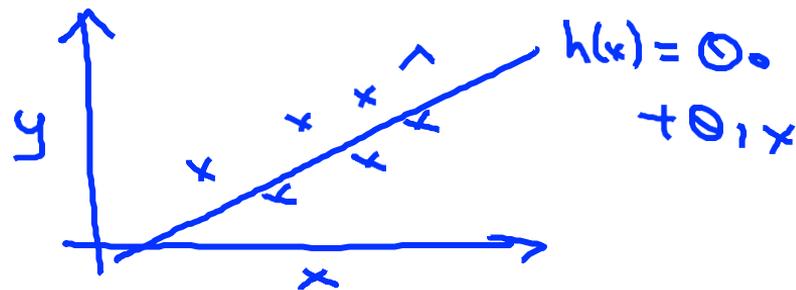
(estimated value of y)

h maps from x 's to y 's.

How do we represent h ?

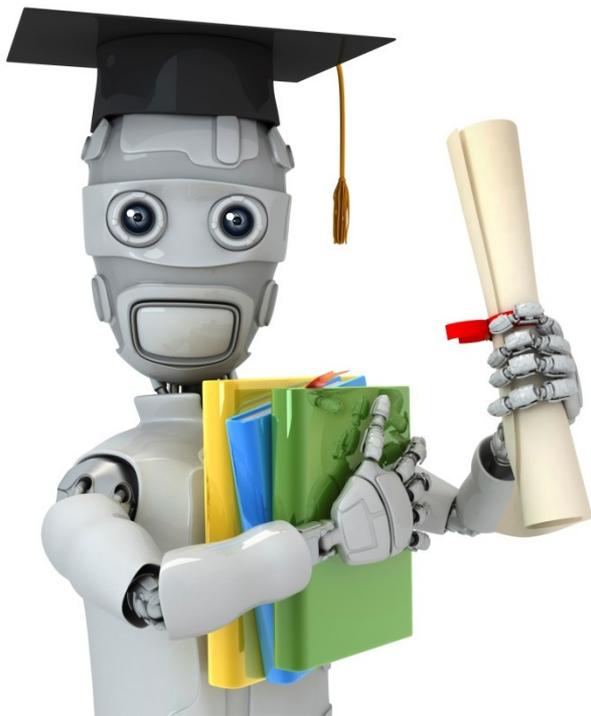
$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

Shorthand: $h(x)$



Linear regression with one variable. (x)
Univariate linear regression.

↳ one variable



Machine Learning

Linear regression
with one variable

Cost function

Training Set

Size in feet ² (x)	Price (\$) in 1000's (y)
2104	460
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...	...

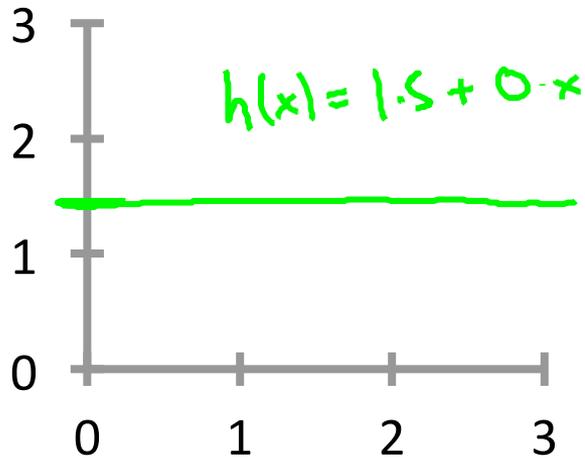
} $n = 47$

Hypothesis: $h_{\theta}(x) = \theta_0 + \theta_1 x$

θ_i 's: Parameters

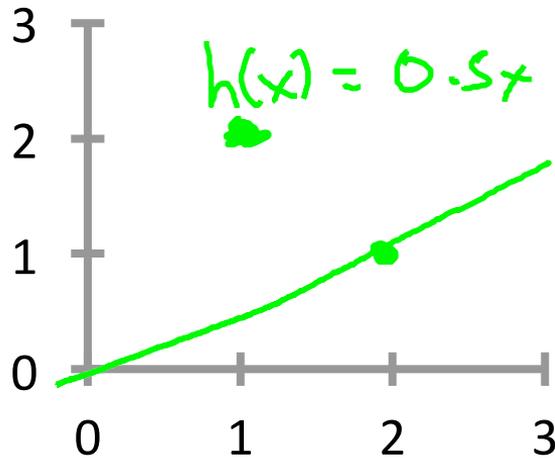
How to choose θ_i 's?

$$\underline{h_{\theta}(x)} = \theta_0 + \theta_1 x$$



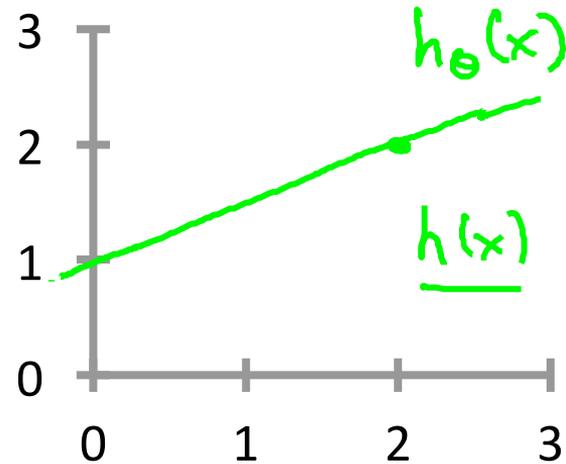
$$\rightarrow \theta_0 = 1.5$$

$$\rightarrow \theta_1 = 0$$



$$\rightarrow \theta_0 = 0$$

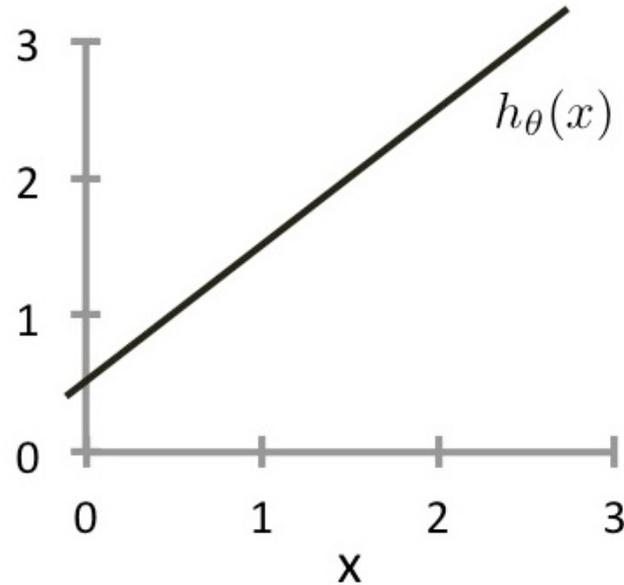
$$\rightarrow \theta_1 = 0.5$$



$$\rightarrow \theta_0 = 1$$

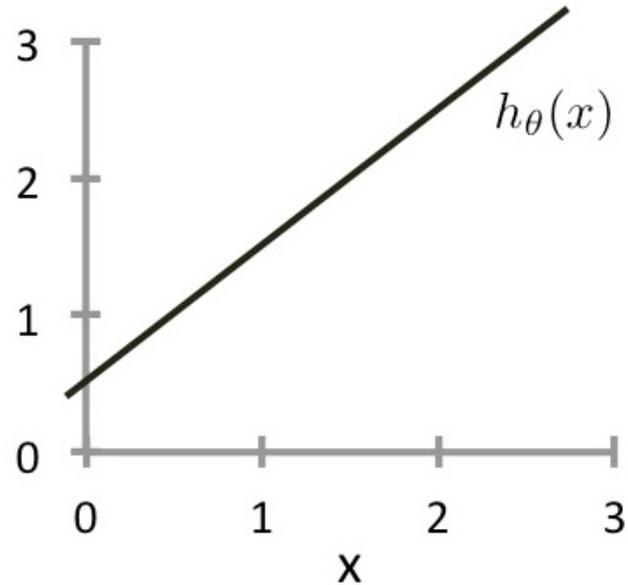
$$\rightarrow \theta_1 = 0.5$$

Consider the plot below of $h_{\theta}(x) = \Theta_0 + \Theta_1 x$. What are Θ_0 and Θ_1 ?

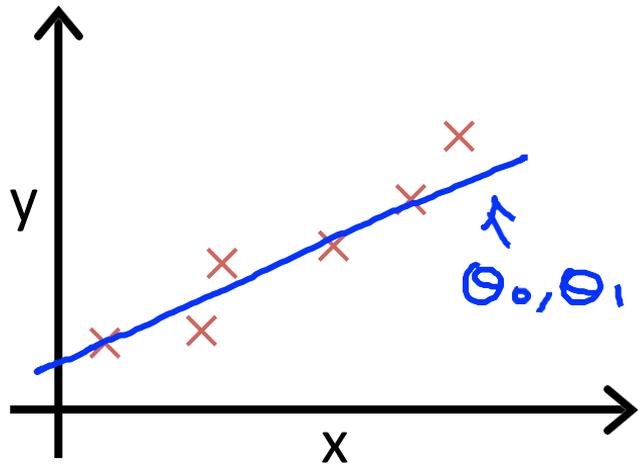


- $\Theta_0 = 0, \Theta_1 = 1$
- $\Theta_0 = 0.5, \Theta_1 = 1$
- $\Theta_0 = 1, \Theta_1 = 0.5$
- $\Theta_0 = 1, \Theta_1 = 1$

Consider the plot below of $h_{\theta}(x) = \Theta_0 + \Theta_1 x$. What are Θ_0 and Θ_1 ?



- $\Theta_0 = 0, \Theta_1 = 1$
- $\Theta_0 = 0.5, \Theta_1 = 1$
- $\Theta_0 = 1, \Theta_1 = 0.5$
- $\Theta_0 = 1, \Theta_1 = 1$



$(x^{(i)}, y^{(i)})$

Idea: Choose θ_0, θ_1 so that $h_\theta(x)$ is close to y for our training examples (x, y)

x, y

minimize θ_0, θ_1

$\frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$

training examples

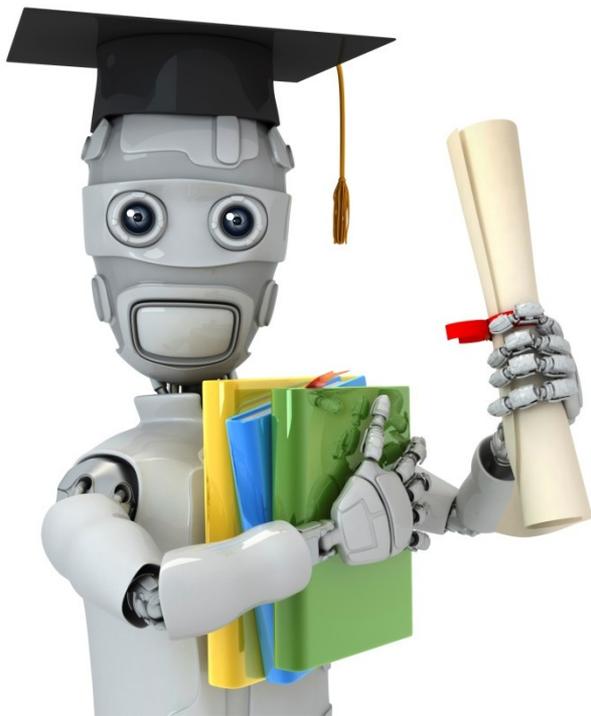
$h_\theta(x^{(i)}) = \theta_0 + \theta_1 x^{(i)}$

$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$

minimize θ_0, θ_1 $J(\theta_0, \theta_1)$

Cost function

Squared error function



Machine Learning

Linear regression
with one variable

Cost function
intuition I

Hypothesis:

$$\underline{h_{\theta}(x) = \theta_0 + \theta_1 x}$$

Parameters:

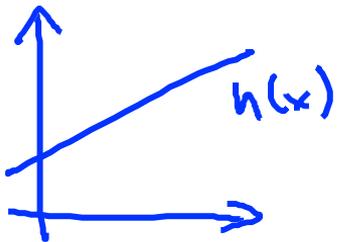
$$\underline{\theta_0, \theta_1}$$

Cost Function:

$$\rightarrow J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

Goal: minimize $J(\theta_0, \theta_1)$

\nearrow θ_0, θ_1

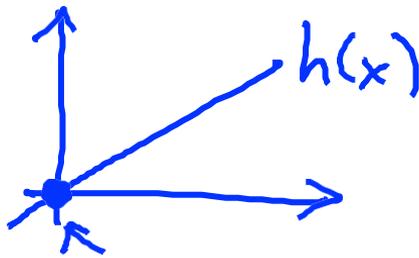


Simplified

$$h_{\theta}(x) = \underline{\theta_1 x}$$

$$\theta_0 = 0$$

$$\underline{\theta_1}$$



$$J(\theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

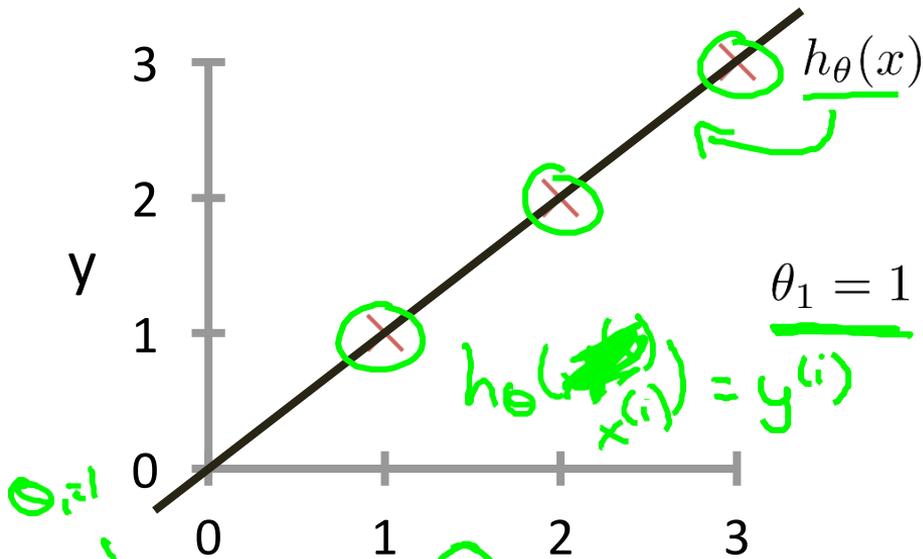
minimize $J(\theta_1)$

$\underline{\theta_1}$

$\theta_1, x^{(i)}$

→ $h_{\theta}(x)$

(for fixed θ_1 , this is a function of x)



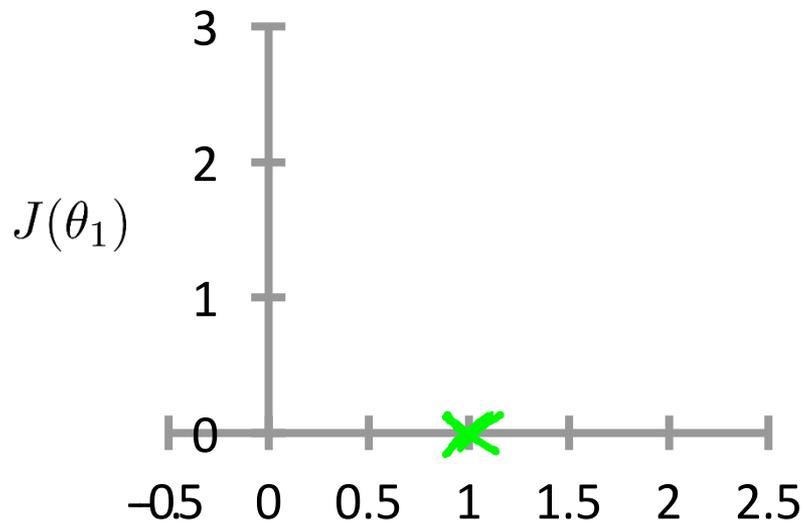
$\theta_1 = 1$

$J(\theta_1) = \frac{1}{2n} \sum_{i=1}^n (h_{\theta}(x^{(i)}) - y^{(i)})^2$

$= \frac{1}{2n} \sum_{i=1}^n (\theta_1 x^{(i)} - y^{(i)})^2 = \frac{1}{2n} (0^2 + 0^2 + 0^2) = 0^2$

→ $J(\theta_1)$

(function of the parameter θ_1)



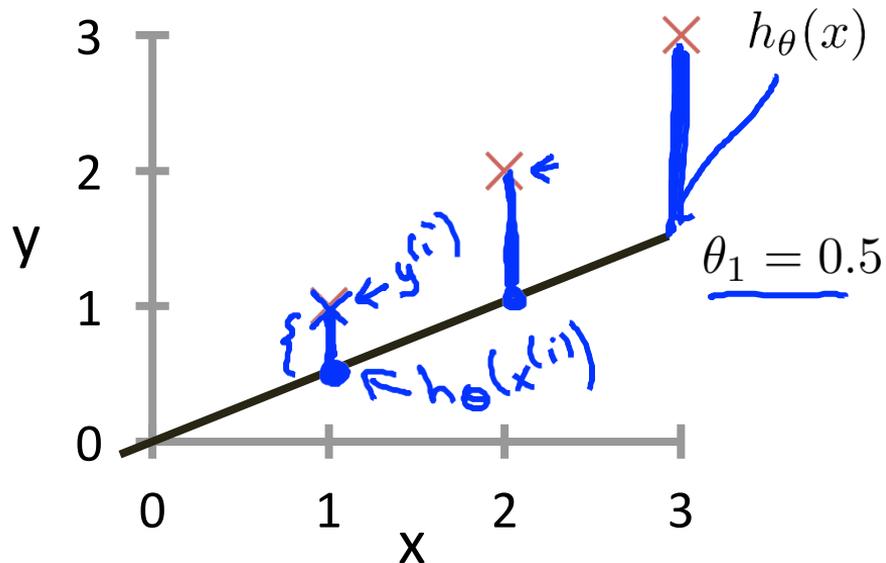
$\theta_1 = 0.5?$

θ_1

$J(1) = 0$

$$h_{\theta}(x)$$

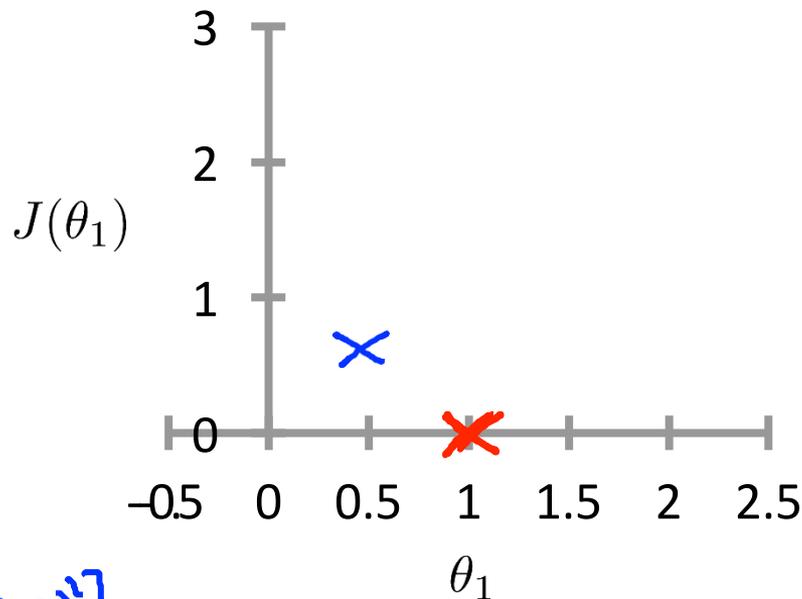
(for fixed θ_1 , this is a function of x)



$$\begin{aligned} J(0.5) &= \frac{1}{2M} [(0.5-1)^2 + (1-2)^2 + (1.5-3)^2] \\ &= \frac{1}{2 \times 3} (3.5) = \frac{3.5}{6} \approx \underline{0.58} \end{aligned}$$

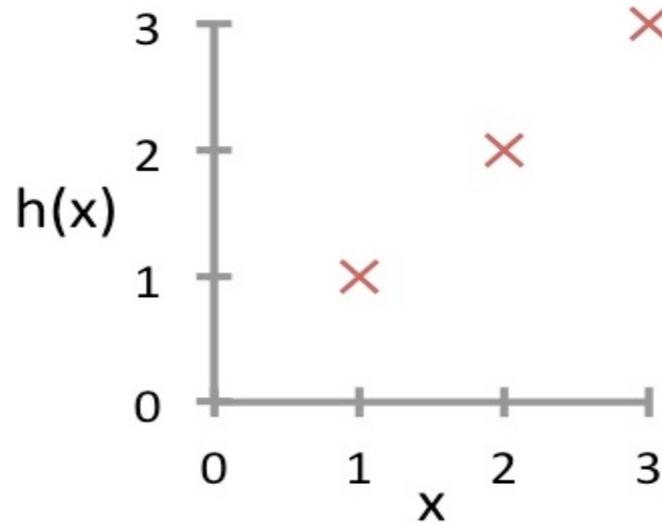
$$J(\theta_1)$$

(function of the parameter θ_1)



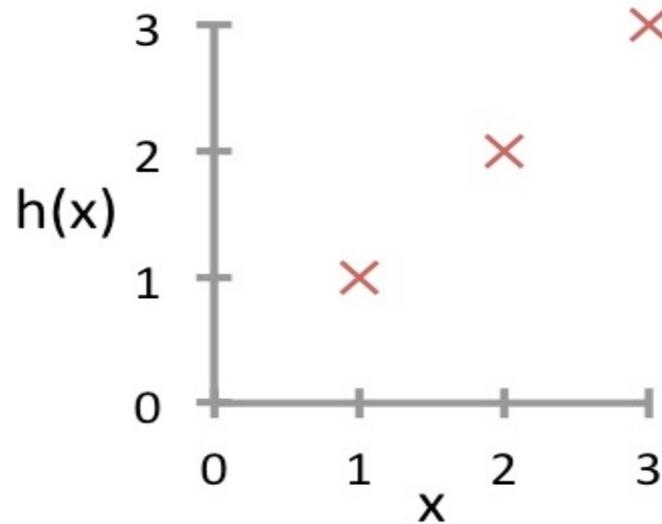
$$\begin{aligned} \theta_1 &= 0? \\ J(0) &=? \end{aligned}$$

Suppose we have a training set with $m=3$ examples, plotted below. Our hypothesis representation is $h_{\theta}(x) = \theta_1 x$, with parameter θ_1 . The cost function $J(\theta_1)$ is $J(\theta_1) = (1/2m) \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$. What is $J(0)$?



- 0
- 1/6
- 1
- 14/6

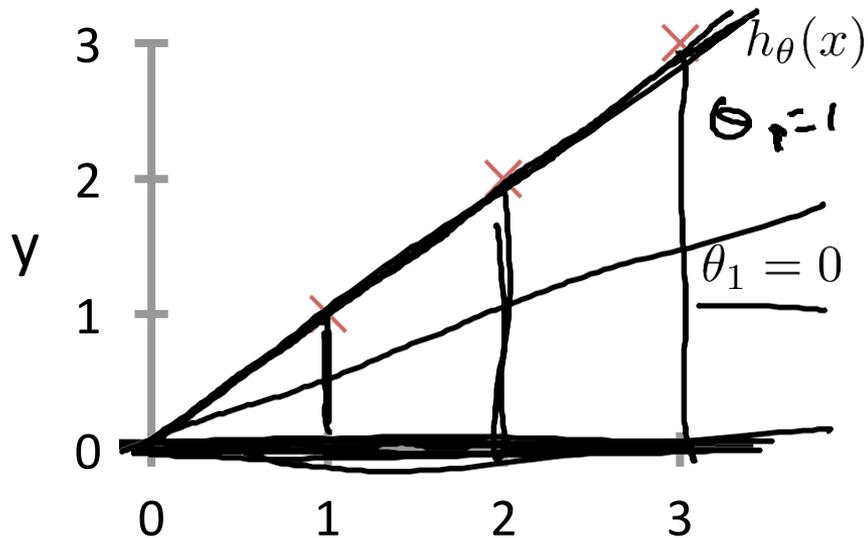
Suppose we have a training set with $m=3$ examples, plotted below. Our hypothesis representation is $h_{\theta}(x) = \theta_1 x$, with parameter θ_1 . The cost function $J(\theta_1)$ is $J(\theta_1) = (1/2m) \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$. What is $J(0)$?



- 0
- 1/6
- 1
- 14/6

$$h_{\theta}(x)$$

(for fixed θ_1 , this is a function of x)



$$J(0) = \frac{1}{2m} (1^2 + 2^2 + 3^2)$$

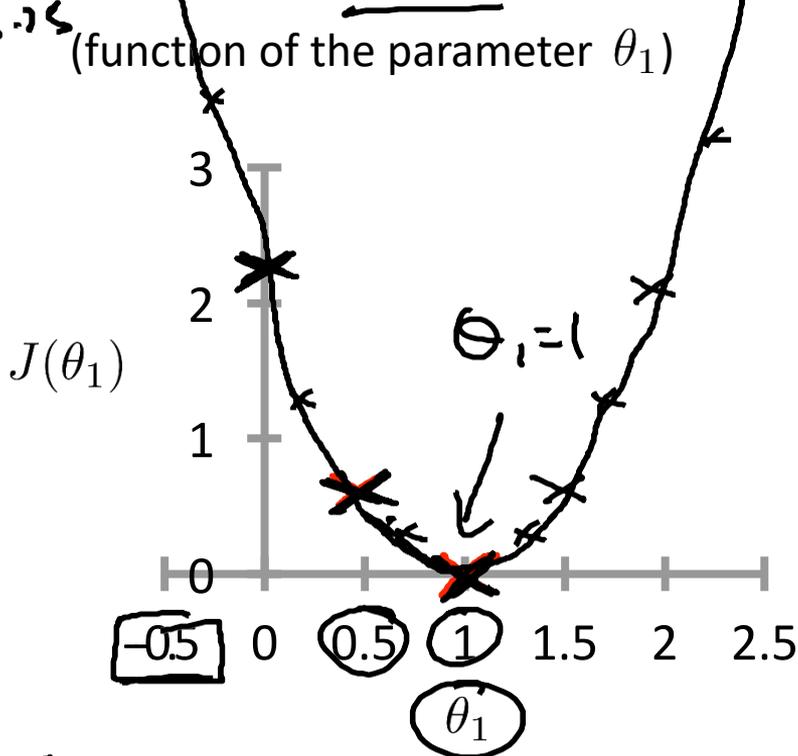
$$= \frac{1}{6} \cdot 14 \approx 2.3$$

$$h(x) = -0.5x$$

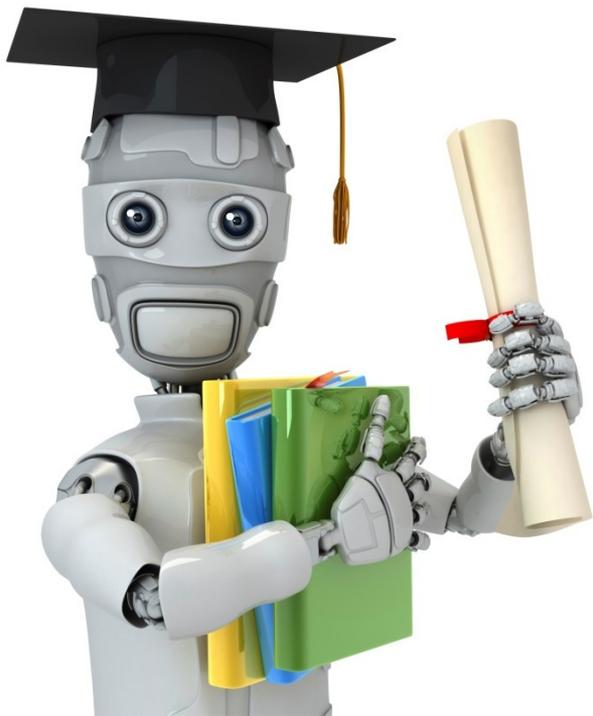
minimize $J(\theta_1)$

$$J(\theta_1)$$

(function of the parameter θ_1)



minimize $J(\theta_1)$



Machine Learning

Linear regression
with one variable

Cost function
intuition II

Hypothesis: $h_{\theta}(x) = \theta_0 + \theta_1 x$

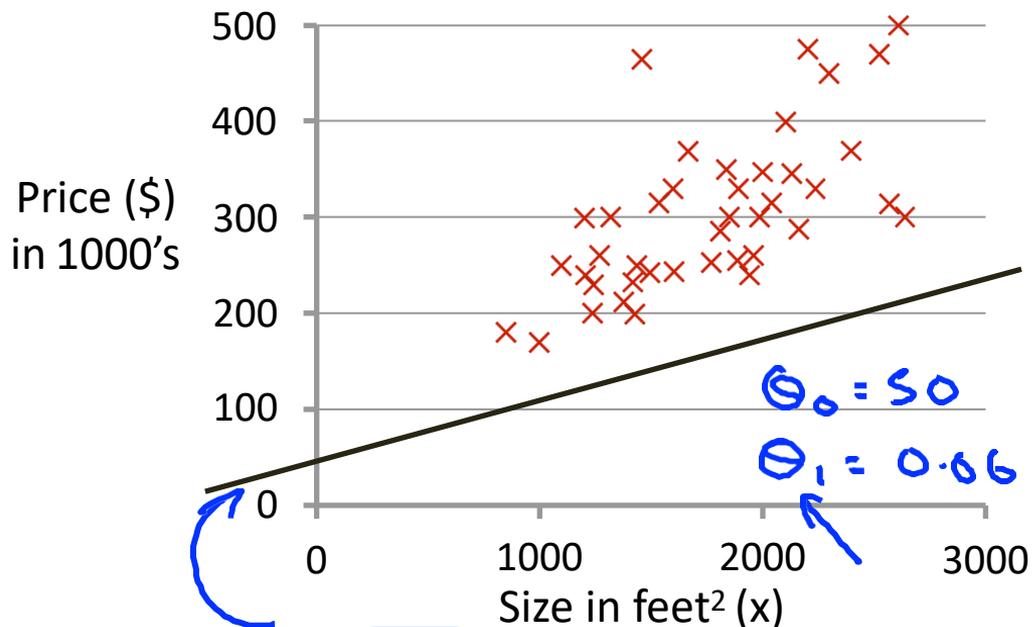
Parameters: θ_0, θ_1

Cost Function: $J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$

Goal: minimize $J(\theta_0, \theta_1)$
 θ_0, θ_1

$$\underline{h_{\theta}(x)}$$

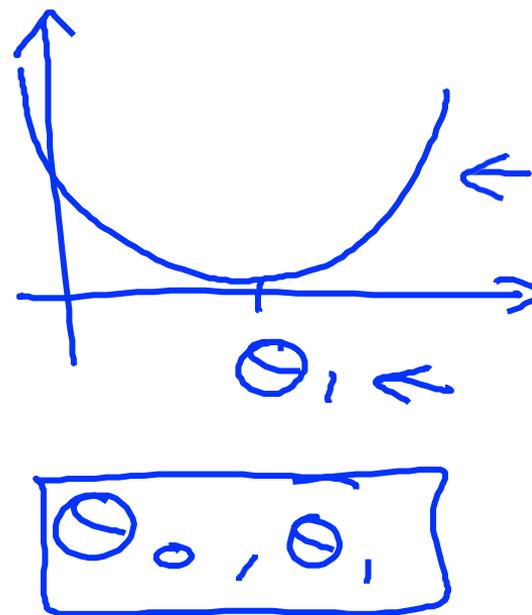
(for fixed θ_0, θ_1 , this is a function of x)



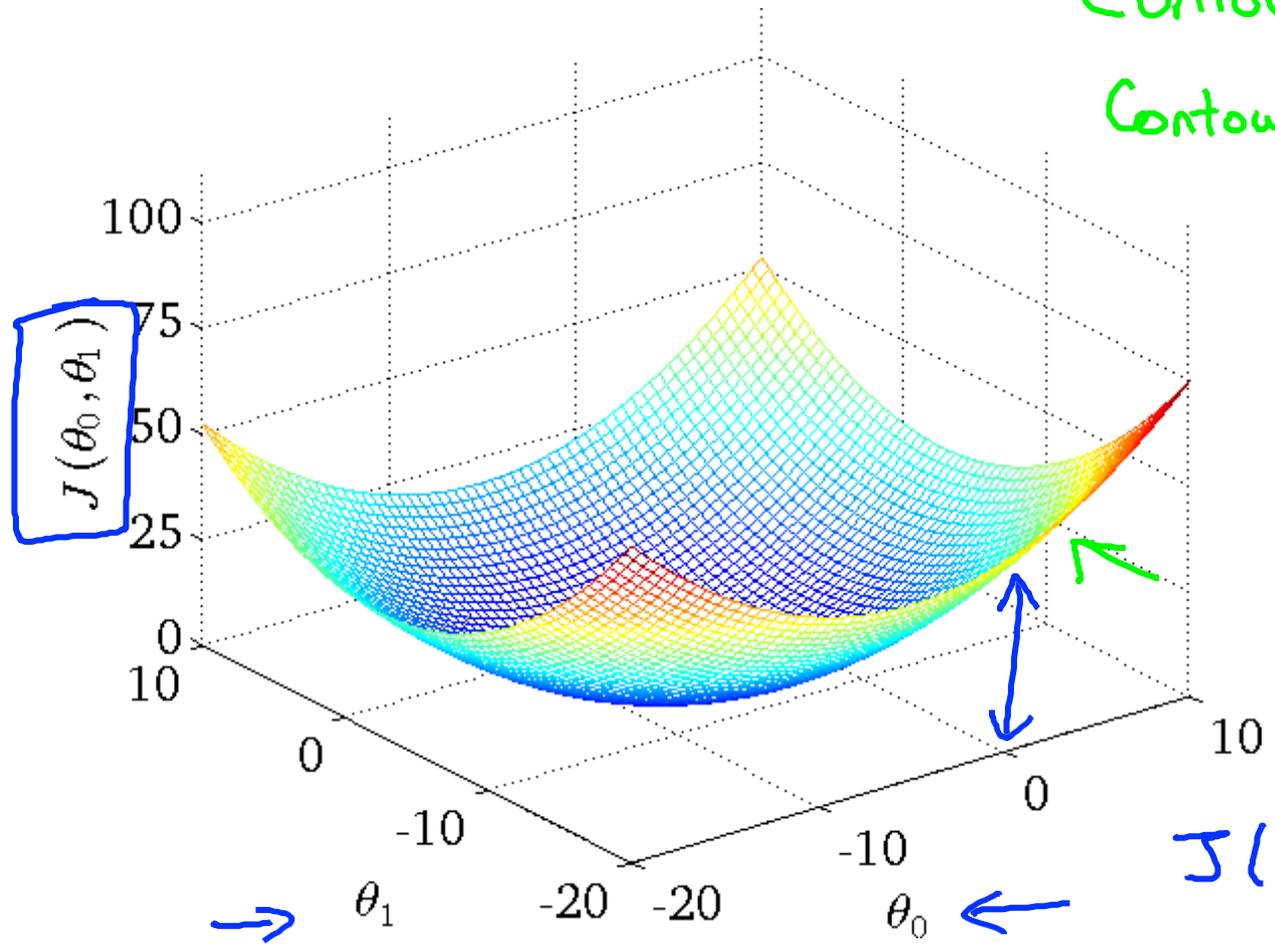
$$h_{\theta}(x) = 50 + 0.06x$$

$$\underline{\underline{J(\theta_0, \theta_1)}}$$

(function of the parameters θ_0, θ_1)



Contour plots
Contour figures -



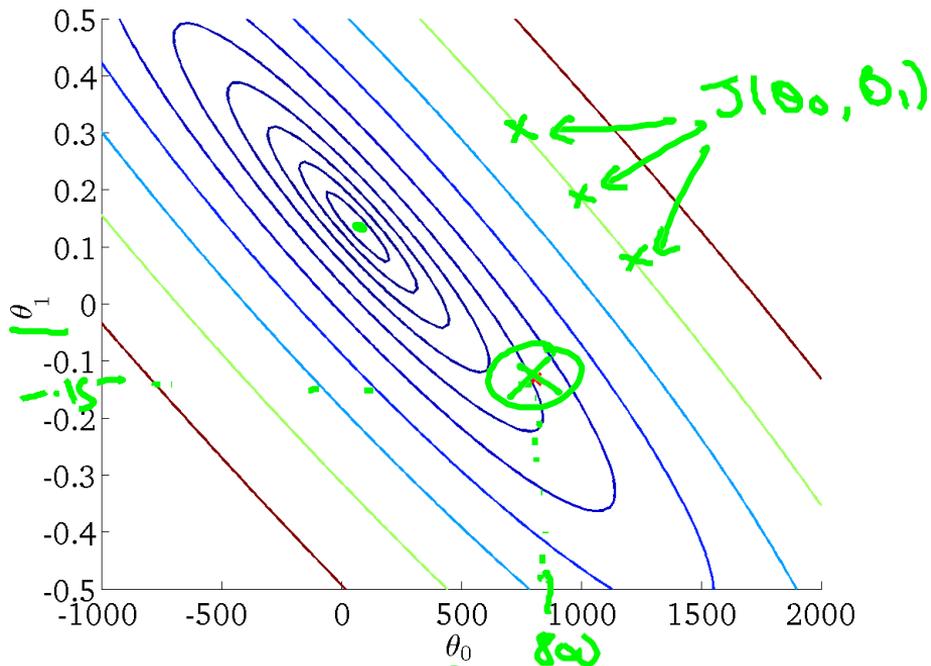
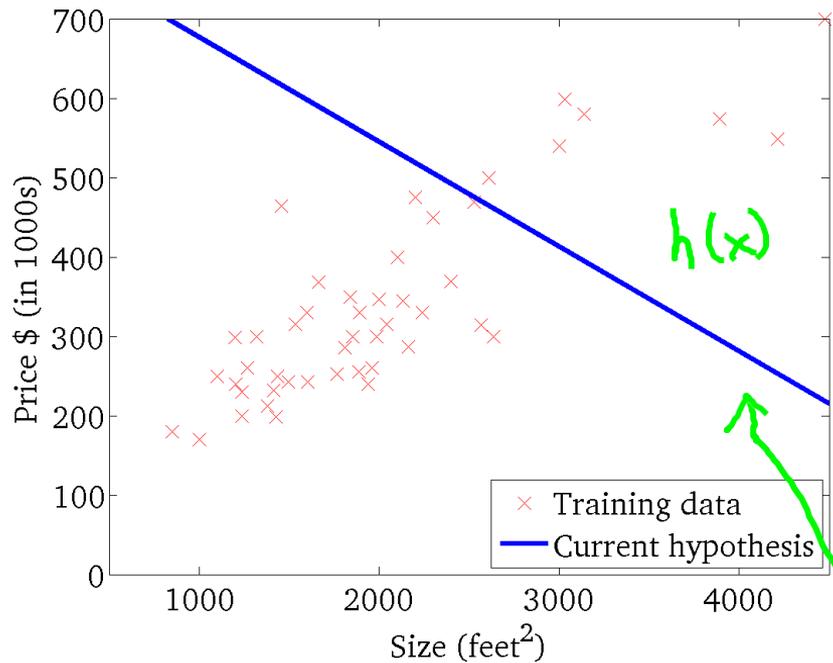
$J(\theta_0, \theta_1)$

$$h_{\theta}(x)$$

$$J(\theta_0, \theta_1)$$

(for fixed θ_0, θ_1 , this is a function of x)

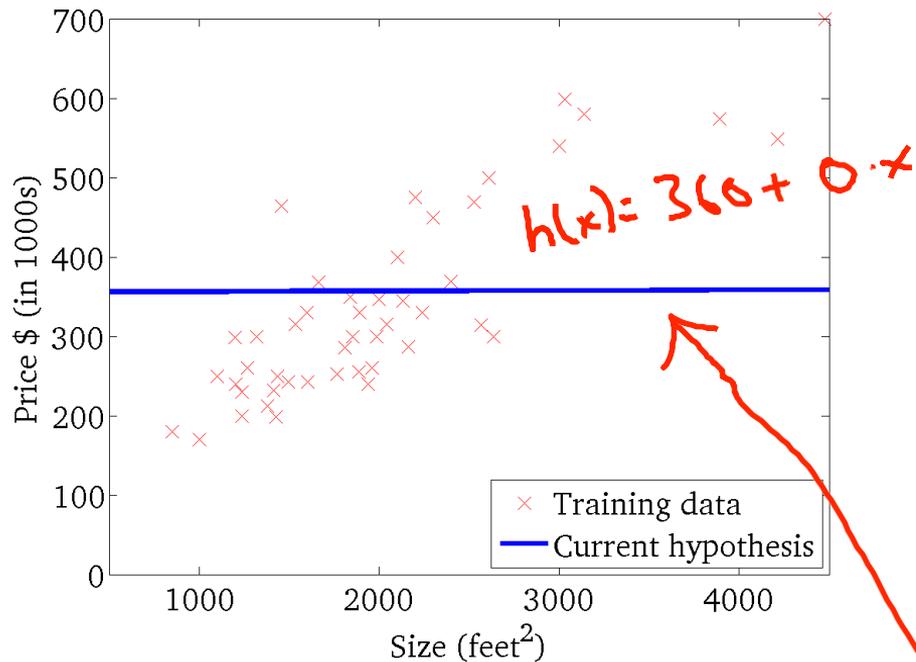
(function of the parameters θ_0, θ_1)



θ_0, θ_1

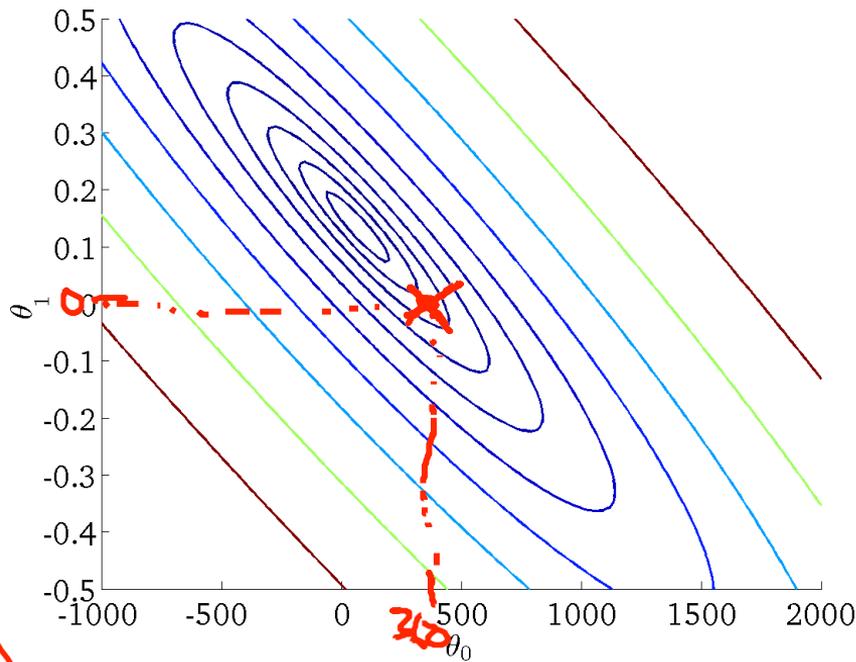
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



$$J(\theta_0, \theta_1)$$

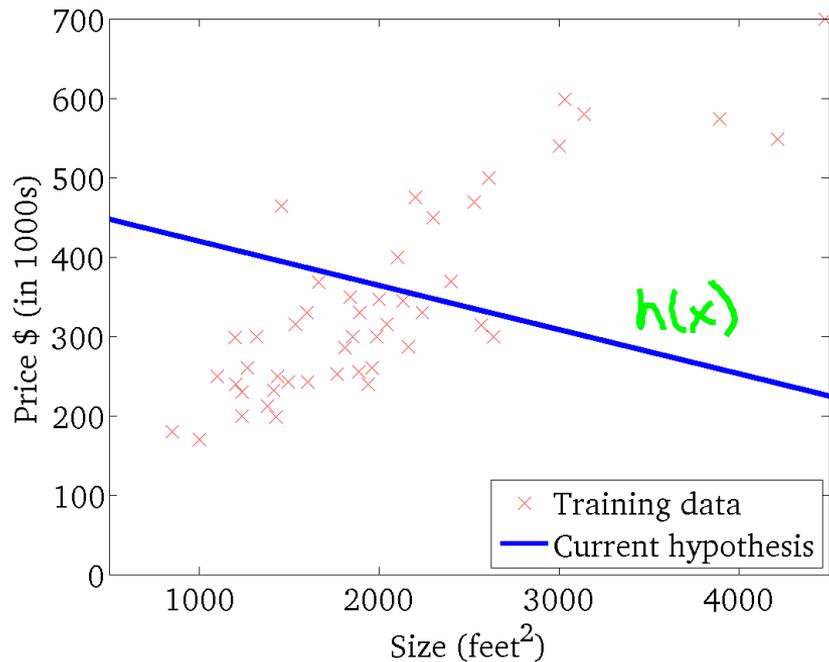
(function of the parameters θ_0, θ_1)



$$\begin{cases} \theta_0 = 360 \\ \theta_1 = 0 \end{cases}$$

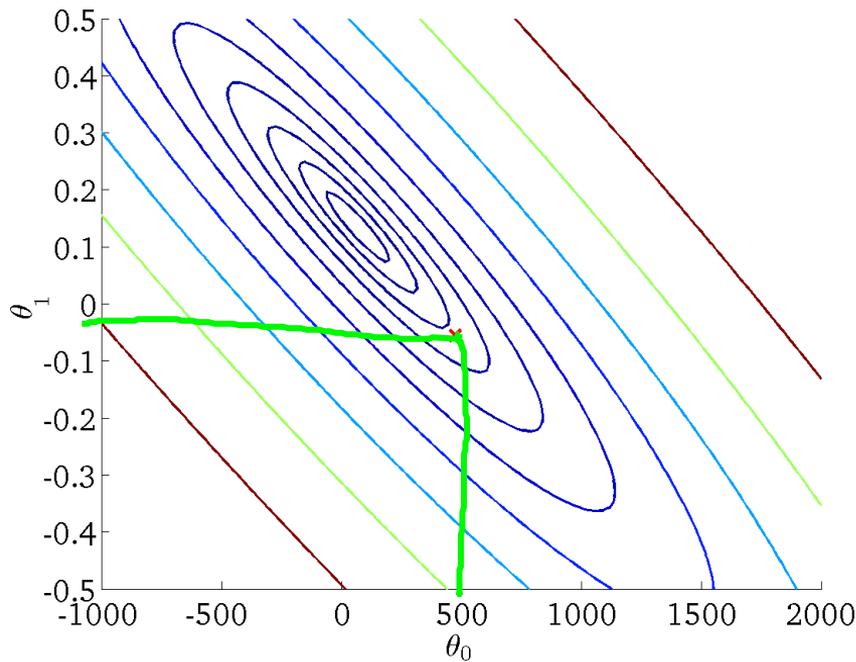
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



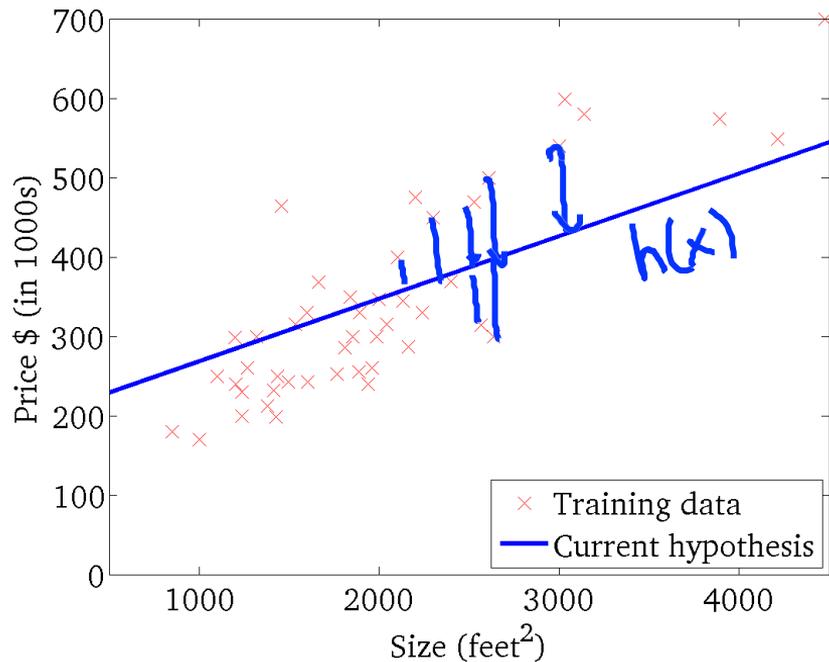
$$J(\theta_0, \theta_1)$$

(function of the parameters θ_0, θ_1)



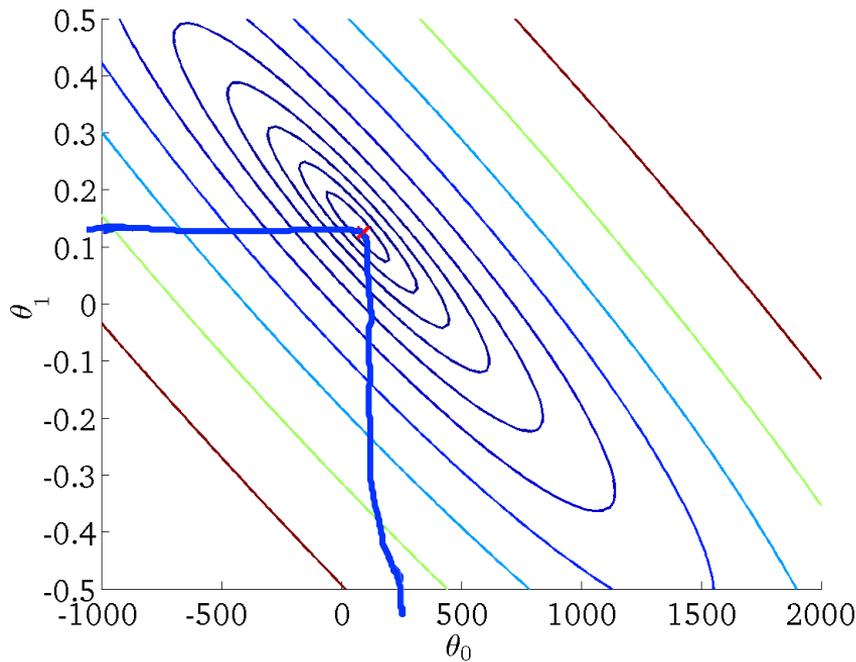
$$h_{\theta}(x)$$

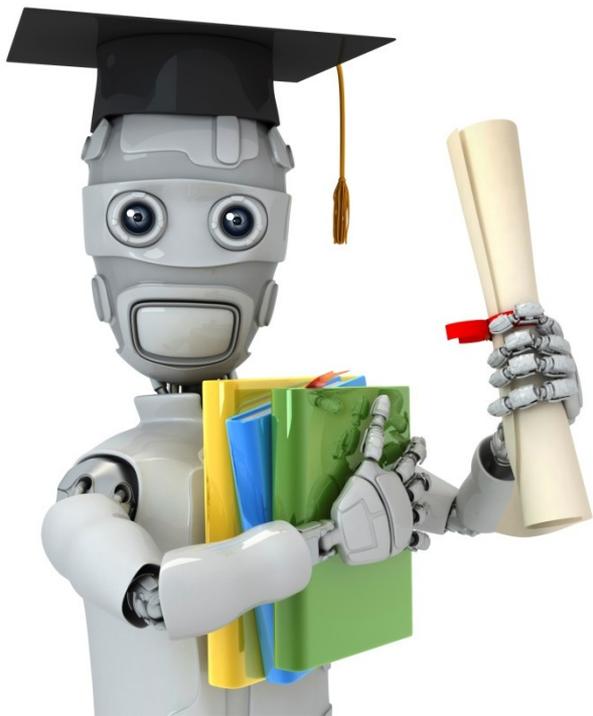
(for fixed θ_0, θ_1 , this is a function of x)



$$J(\theta_0, \theta_1)$$

(function of the parameters θ_0, θ_1)





Machine Learning

Linear regression
with one variable

Next Seminar

Gradient

descent