

# High-Performance Computing for Atomistic Materials Modeling

Steve Plimpton  
Sandia National Labs

HPC Symposium 2012  
Lehigh University - March 2012



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See you at the movies ...



# CGI modeling advances by Pixar



Bug's Life (1998)  
**vegetation**



Monsters, Inc (2001)  
**hair**



Finding Nemo (2003)  
**water**



Cars (2006)  
**painted surfaces**



Ratatouille (2007)  
**food**



Wall-E (2008)  
**rust & decay**

- Faster computers enable better models
- “Law of Constancy of Pain”
- Adept at discarding low-level details
- Animations “look” right
- Success due to more than modeling, tell a good story
- Ultimate goal: fast & realistic modeling of any material with minimum of effort by user

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- 
- Bottom line: 12 films, \$600M/film, 21 Academy Awards

## Pixar vs HPC materials modeling

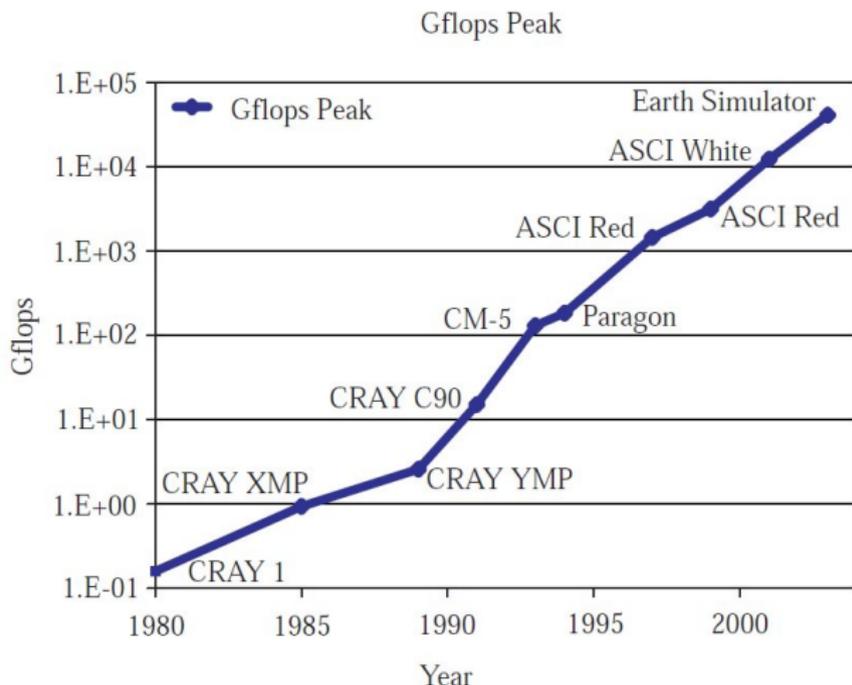
- Faster computers enable better models
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- Animations “look” right  $\Rightarrow$  **Simulations match experiment**
- Success due to more than modeling, tell a good **science** story
- Ultimate goal: fast & realistic modeling of any material with minimum of effort by simulator

# Pixar vs HPC materials modeling

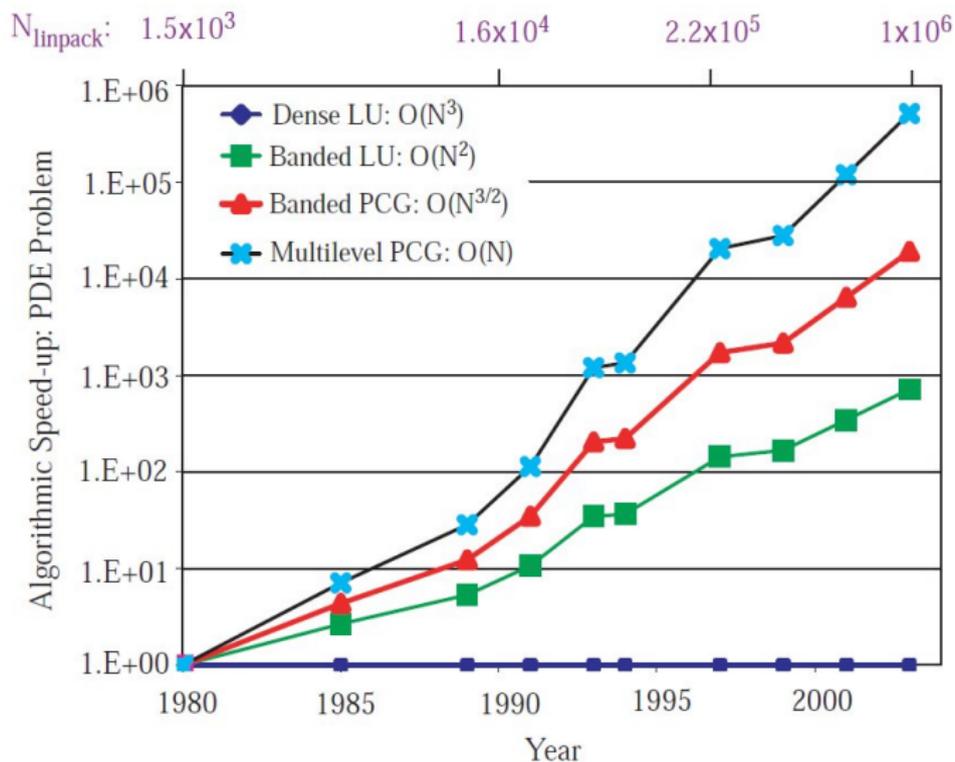
- Faster computers enable better models
  - “Law of Constancy of Pain”
  - Adept at discarding low-level details
  - Animations “look” right ⇒ **Simulations match experiment**
  - Success due to more than modeling, tell a good **science** story
  - Ultimate goal: fast & realistic modeling of any material with minimum of effort by simulator
- 
- Bottom line: \$600M/**grant**, 21 Academy Awards (**sorry**)

# Machines are getting faster (and harder to use)

1 Petaflop in 2008, now at **10 Petaflops**



# PDE matrix solvers are getting more clever

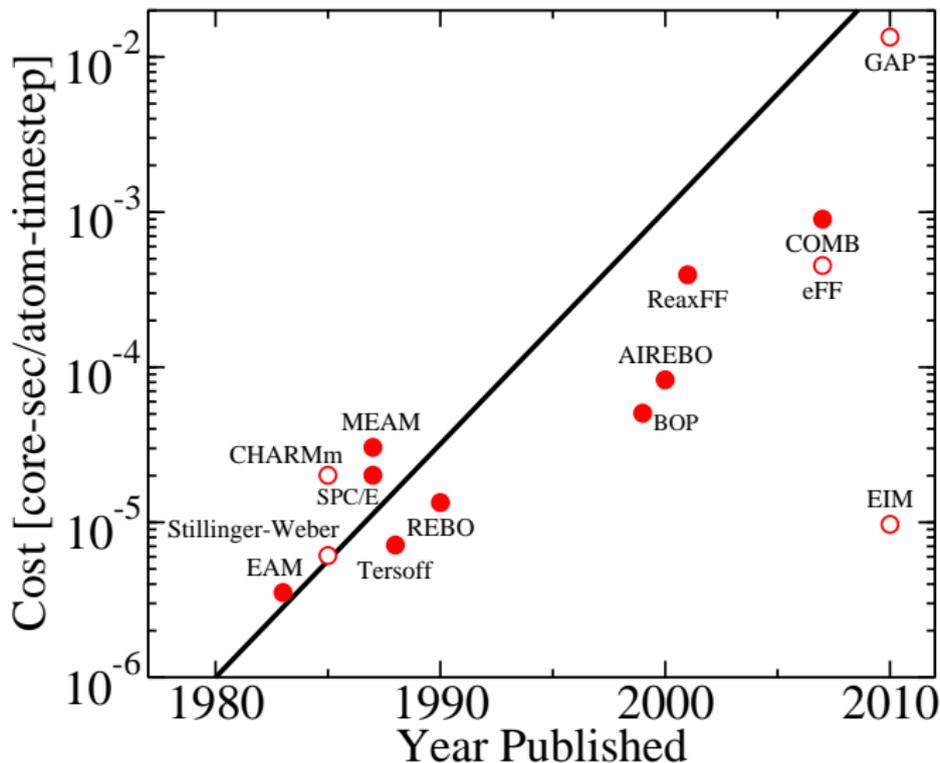


# Empirical potentials are getting more clever and costly!

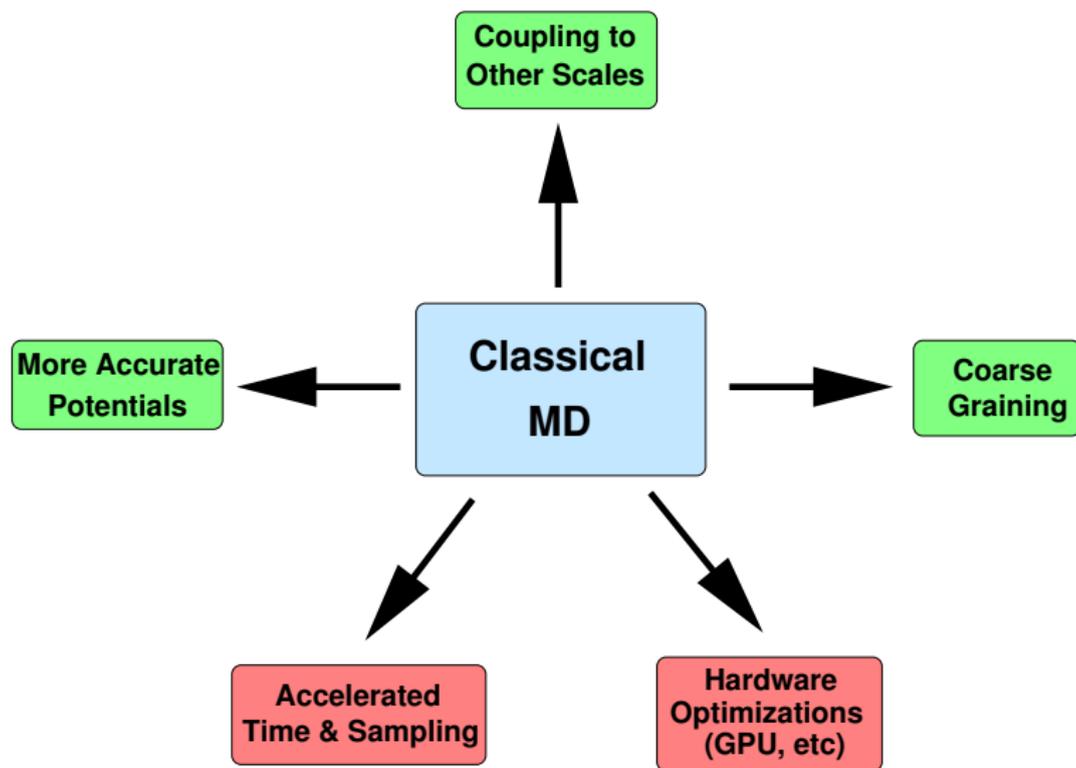
See [lammps.sandia.gov/bench.html#potentials](http://lammps.sandia.gov/bench.html#potentials)

Potential	System	Atoms	Timestep	CPU	LJ Ratio
Granular	chute flow	32000	0.0001 tau	5.08e-7	0.34x
FENE bead/spring	polymer melt	32000	0.012 tau	5.32e-7	0.36x
Lennard-Jones	LJ liquid	32000	0.005 tau	1.48e-6	1.0x
DPD	pure solvent	32000	0.04 tau	2.16e-6	1.46x
EAM	bulk Cu	32000	5 fmsec	3.59e-6	2.4x
Tersoff	bulk Si	32000	1 fmsec	6.01e-6	4.1x
Stillinger-Weber	bulk Si	32000	1 fmsec	6.10e-6	4.1x
EIM	crystalline NaCl	32000	0.5 fmsec	9.69e-6	6.5x
SPC/E	liquid water	36000	2 fmsec	1.43e-5	9.7x
CHARMM + PPPM	solvated protein	32000	2 fmsec	2.01e-5	13.6x
MEAM	bulk Ni	32000	5 fmsec	2.31e-5	15.6x
Peridynamics	glass fracture	32000	22.2 nsec	2.42e-5	16.4x
Gay-Berne	ellipsoid mixture	32768	0.002 tau	4.09e-5	28.3x
AIREBO	polyethylene	32640	0.5 fmsec	8.09e-5	54.7x
COMB	crystalline SiO2	32400	0.2 fmsec	4.19e-4	284x
eFF	H plasma	32000	0.001 fmsec	4.52e-4	306x
ReaxFF	PETN crystal	16240	0.1 fmsec	4.99e-4	337x
ReaxFF/C	PETN crystal	32480	0.1 fmsec	2.73e-4	185x
VASP/small	water	192/512	0.3 fmsec	26.2	17.7e6
VASP/medium	CO2	192/1024	0.8 fmsec	252	170e6
VASP/large	Xe	432/3456	2.0 fmsec	1344	908e6

# Moore's Law for potentials



# Research directions in classical MD, enabled by HPC



# Particle suspensions

- **Colloids** = large particles, sub-micron to few microns in diameter, squishy or hard, bare or coated, spherical or irregular in shape
- **Nanoparticles** = small colloids, 2-100 nm in diameter
- **Suspension** = background fluid

# Particle suspensions

- **Colloids** = large particles, sub-micron to few microns in diameter, squishy or hard, bare or coated, spherical or irregular in shape
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- Applications:

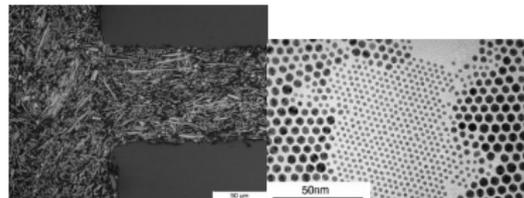
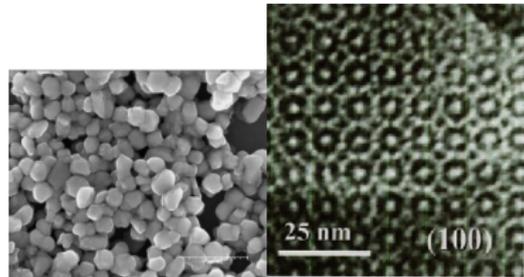
- bulk: paints, gels, pastes
- films: self-assembly of nano-structured materials

- Processing steps:

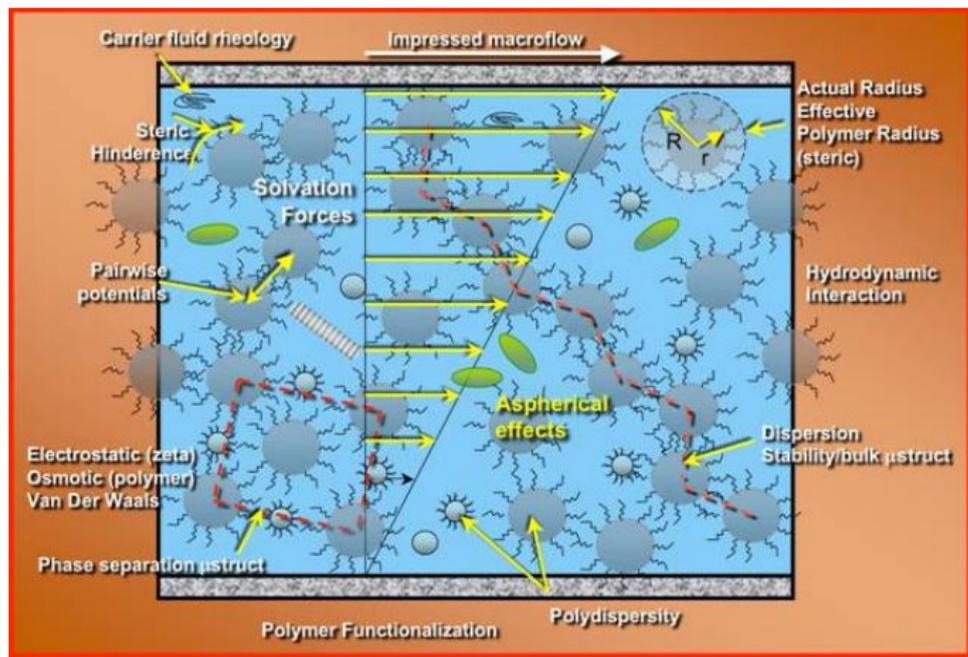
- extrusion, flow, drying, self-assembly

- Measure/predict:

- **diffusion**, **rheology**, aggregation/dispersion

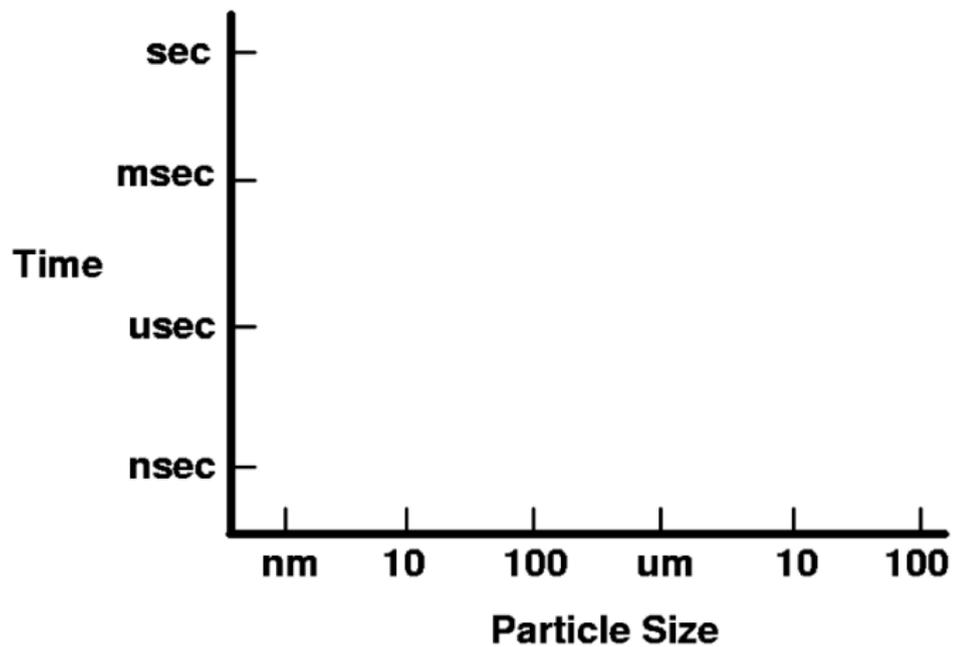


# What we want to model

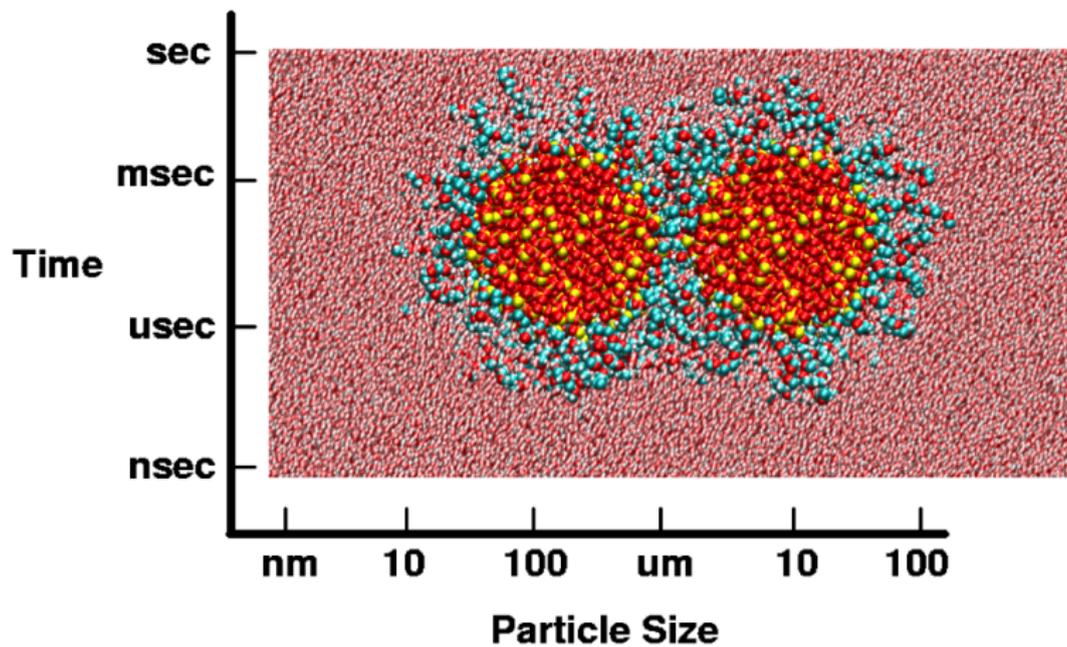


Spherical vs aspherical, bare vs coated, polydisperse, agglomeration, response to shear, ...

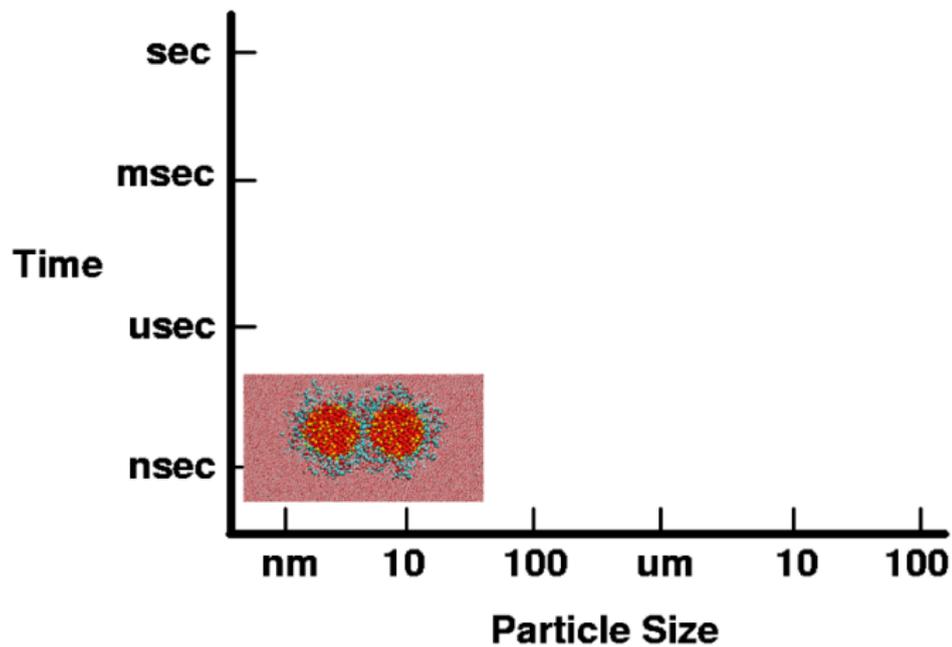
## Length and time scales



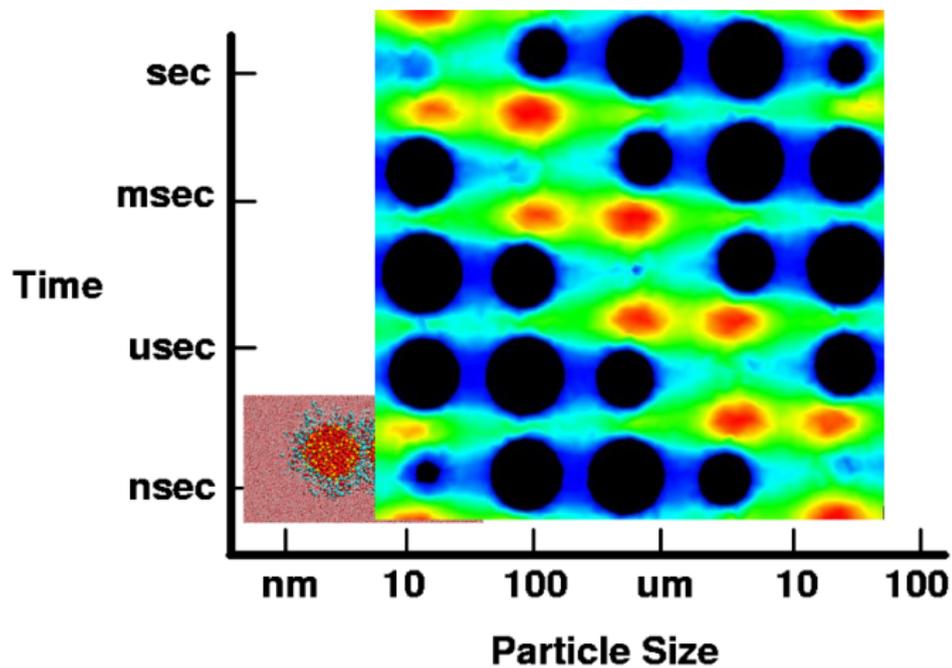
# Length and time scales



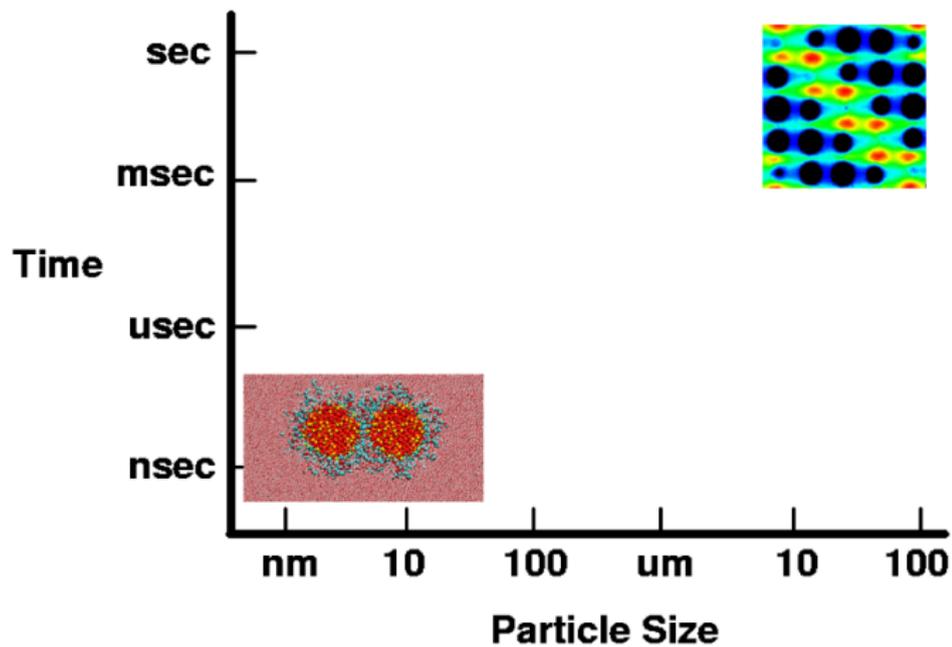
# Length and time scales



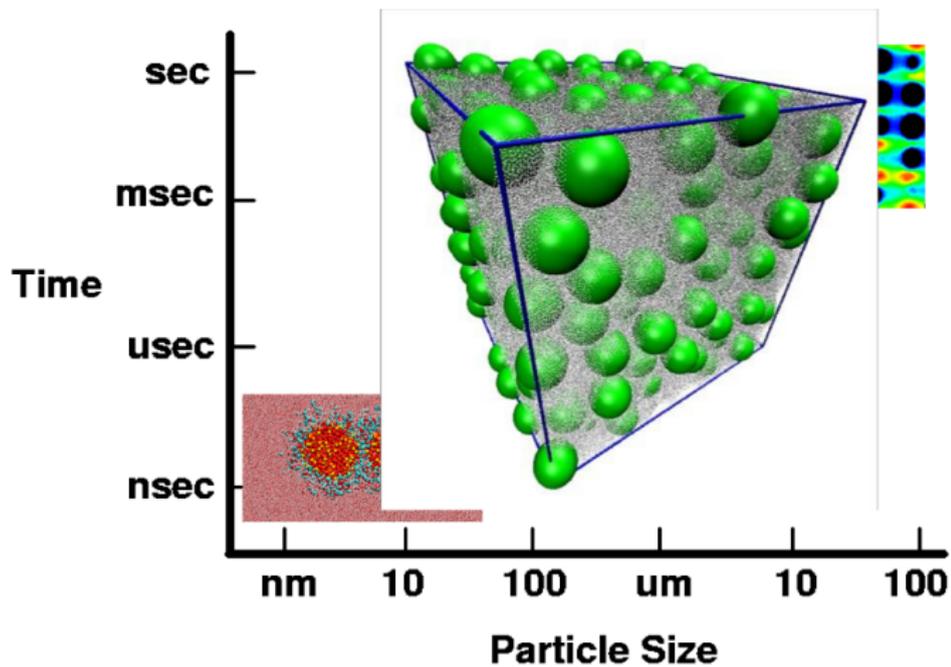
# Length and time scales



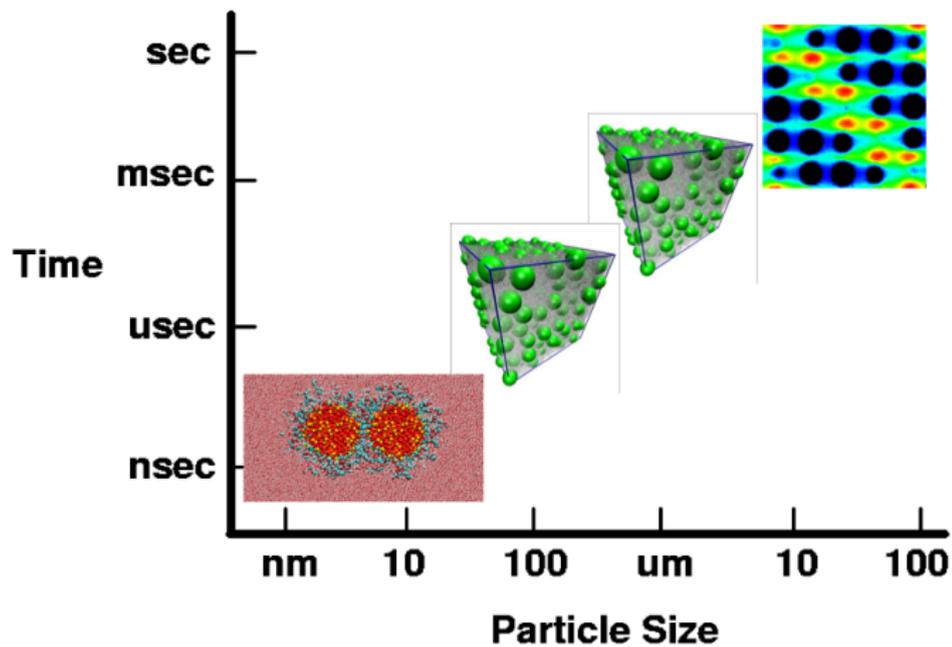
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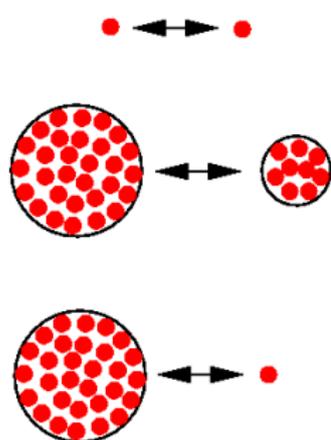


# Length and time scales



# Coarse-grained nanoparticle interactions

- Integrated LJ potential over volume of nanoparticle  
*Everaers (PRE 2003)*



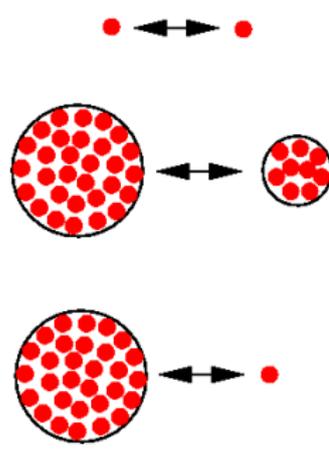
$$U_A = -\frac{A_{cc}}{6} \left[ \frac{2a_1a_2}{r^2 - (a_1 + a_2)^2} + \frac{2a_1a_2}{r^2 - (a_1 - a_2)^2} + \ln \left( \frac{r^2 - (a_1 + a_2)^2}{r^2 - (a_1 - a_2)^2} \right) \right]$$

$$U_R = \frac{A_{cc}}{37800} \frac{\sigma^6}{r} \left[ \frac{r^2 - 7r(a_1 + a_2) + 6(a_1^2 + 7a_1a_2 + a_2^2)}{(r - a_1 - a_2)^7} + \frac{r^2 + 7r(a_1 + a_2) + 6(a_1^2 + 7a_1a_2 + a_2^2)}{(r + a_1 + a_2)^7} - \frac{r^2 + 7r(a_1 - a_2) + 6(a_1^2 - 7a_1a_2 + a_2^2)}{(r + a_1 - a_2)^7} - \frac{r^2 - 7r(a_1 - a_2) + 6(a_1^2 - 7a_1a_2 + a_2^2)}{(r - a_1 + a_2)^7} \right]$$

$$U = U_A + U_R, \quad r < r_c$$

# Coarse-grained nanoparticle interactions

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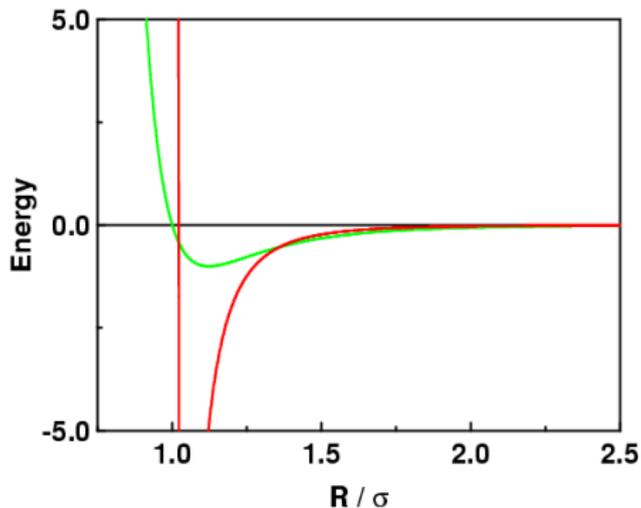
$$U_A = -\frac{A_{cc}}{6} \left[ \frac{2a_1 a_2}{r^2 - (a_1 + a_2)^2} + \frac{2a_1 a_2}{r^2 - (a_1 - a_2)^2} + \ln \left( \frac{r^2 - (a_1 + a_2)^2}{r^2 - (a_1 - a_2)^2} \right) \right]$$

$$U_R = \frac{A_{cc}}{37800} \frac{\sigma^6}{r} \left[ \frac{r^2 - 7r(a_1 + a_2) + 6(a_1^2 + 7a_1 a_2 + a_2^2)}{(r - a_1 - a_2)^7} + \frac{r^2 + 7r(a_1 + a_2) + 6(a_1^2 + 7a_1 a_2 + a_2^2)}{(r + a_1 + a_2)^7} - \frac{r^2 + 7r(a_1 - a_2) + 6(a_1^2 - 7a_1 a_2 + a_2^2)}{(r + a_1 - a_2)^7} - \frac{r^2 - 7r(a_1 - a_2) + 6(a_1^2 - 7a_1 a_2 + a_2^2)}{(r - a_1 + a_2)^7} \right]$$

$$U = U_A + U_R, \quad r < r_c$$

- Pairwise and analytic (albeit expensive), **Hamaker constant**, similar formulation for ellipsoids

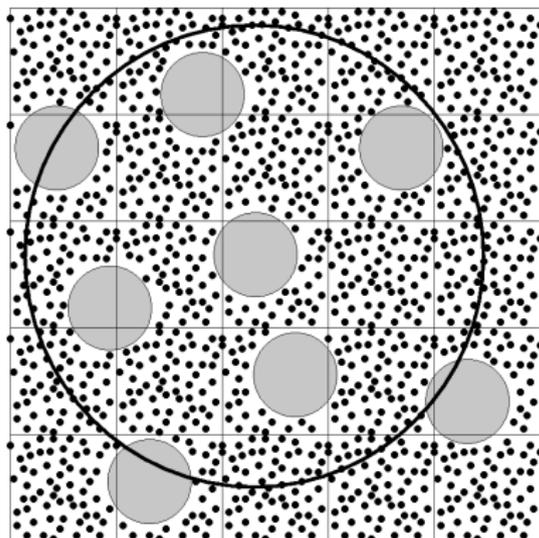
# Colloid/colloid forces are now long-range



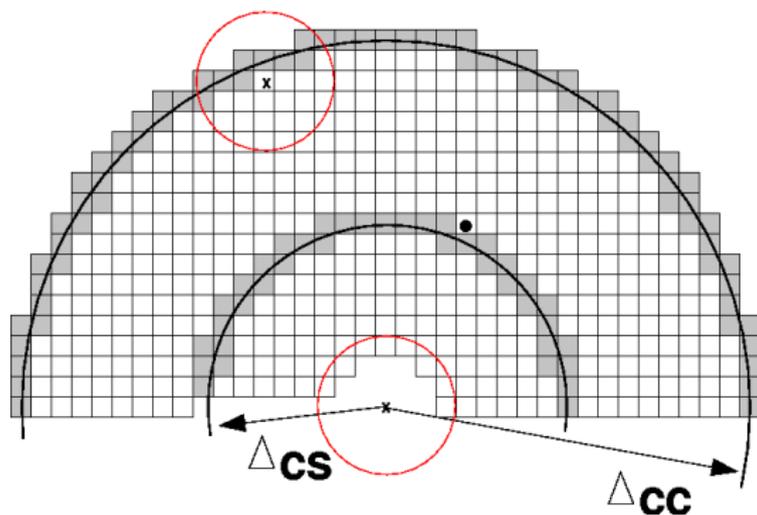
- Distance is plotted in particle diameters
- For colloid/solvent size ratio of 20:1, LJ cutoff of **2.5 sigma** translates to: colloid/colloid cutoff = **50 sigma**, colloid/solvent cutoff = **25 sigma**

# Finding neighbors in mixtures

- Goal: efficient Verlet lists
  - SS cutoff at 2.5
  - CS cutoff at 12.5
  - CC cutoff at 25
- Bin size = 1/2 of max cutoff
- Problem: compute  $R_{ij}$  for too many pairs
- Performance:  
0.5M particles, 100 S/C
  - 4.7 secs (pair)
  - **242 secs (neighbor)**
  - **36 secs (communication)**
- Exacerbated as size ratio grows



## Faster neighbor finding



- Bin based on smallest cutoff
- Store 2 values with each stencil bin (closest/furthest corners)
- Only need compute  $R_{ij}$  in shaded ring/shell of bins
- Improved performance:  
4.7 secs (pair), **2.4 secs (neigh)**, **2.1 secs (comm)**

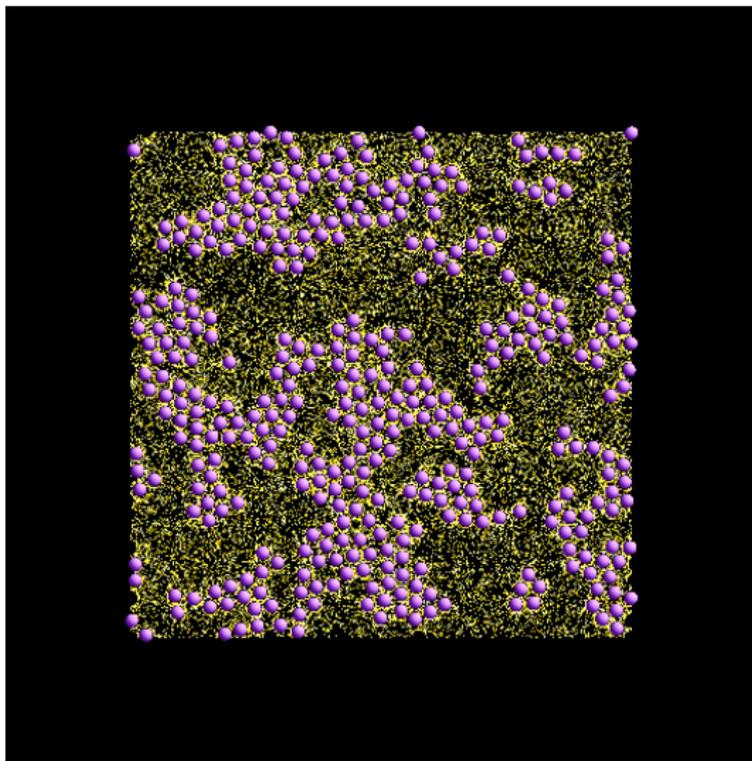
# Performance improvement

3 size ratios, 3 volume fractions, CPU time for 100 steps

Ratio	P	N	old/old	new/old	new/new
5:1	27	200K	17.8	6.8	5.4
		143K	7.6	4.0	3.1
		87K	3.0	2.0	1.6
10:1	64	672K	471	19.2	11.2
		558K	284	15.9	8.2
		445K	165	11.3	5.6
20:1	125	2.3M	5630	88.6	38.6
		2.0M	4390	73.7	31.2
		1.7M	2750	56.9	22.0

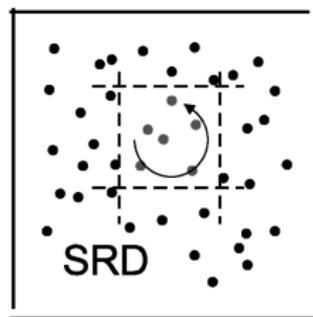
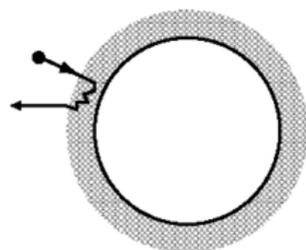
Bottom line: new algorithms as much as **100x faster**

# Shear of polymer chains



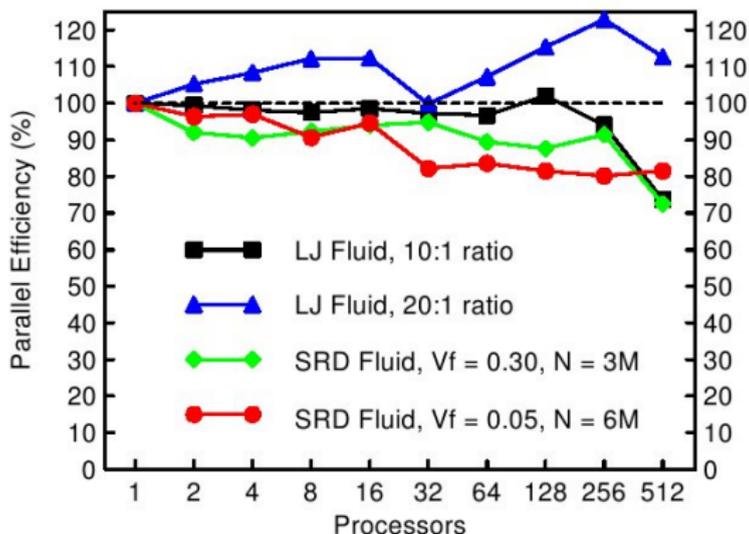
# Further coarse graining via SRD particles

- SRD = **stochastic rotation dynamics**
  - *Malevanets (J Chem Phys 99), Padding (PRL 04), Hecht (PRE 05)*
  - intermediate Peclet numbers  $\sim 1$   
 $Pe = \text{ratio of advection to diffusion}$
- Basic idea:
  - SRDs are background solvent for colloids
  - two timescales:  $t_{colloid}$  and  $t_{SRD}$
  - **small**  $t_{colloid}$ :
    - colloids move, C/C interactions
    - SRDs advect (no self-interactions)
    - detect colloid-SRD collisions
  - **large**  $t_{SRD}$ :
    - bin SRDs,  $v$  is randomly rotated



# Parallel performance

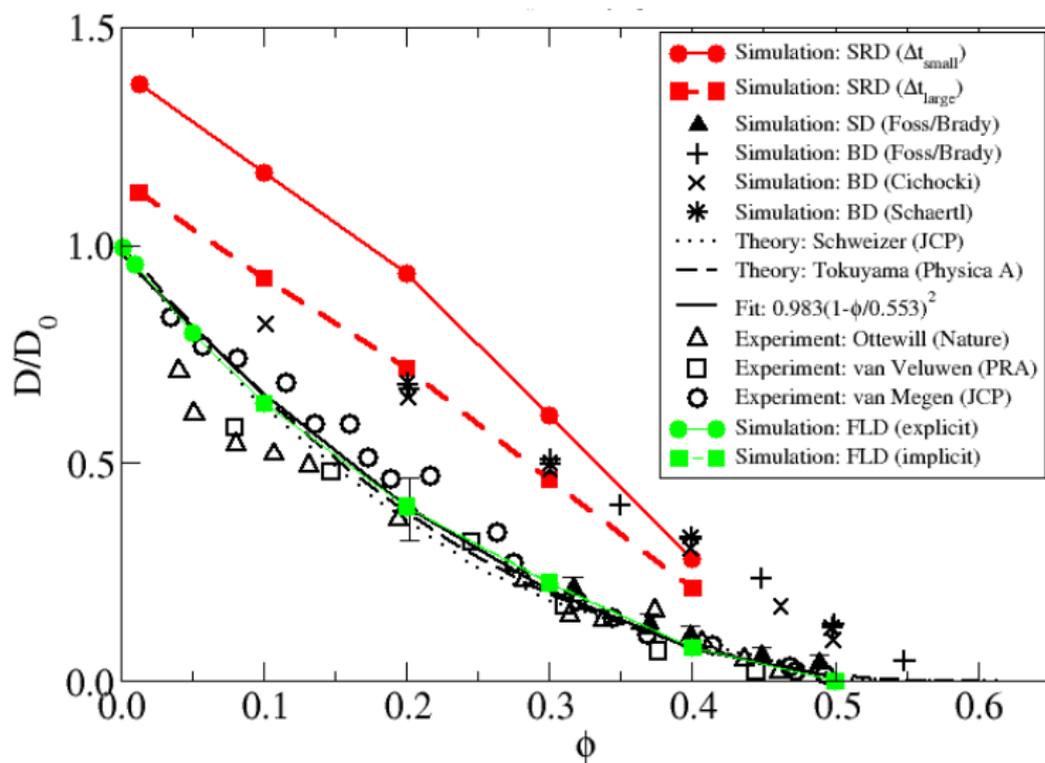
- Key point: SRDs are **cheap** due to no S/S interactions
- Challenge: Keep them cheap when 1000s per colloid



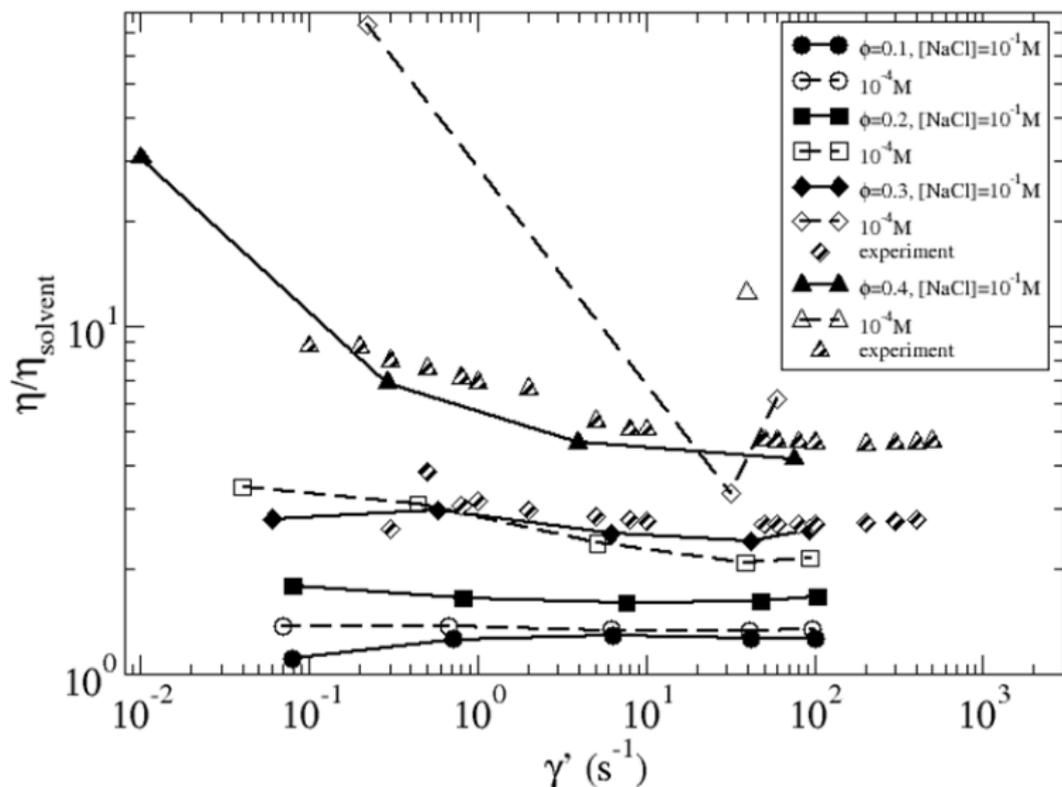
Savings vs explicit LJ solvent:

**30x** in speed (per particle), **20x** in timestep

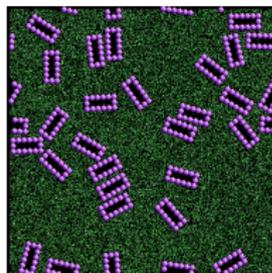
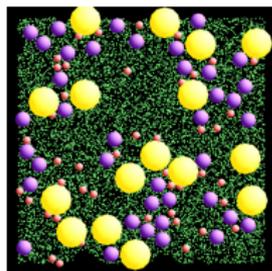
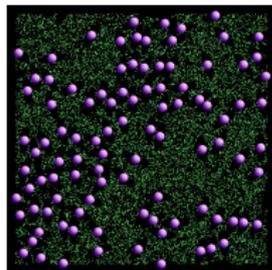
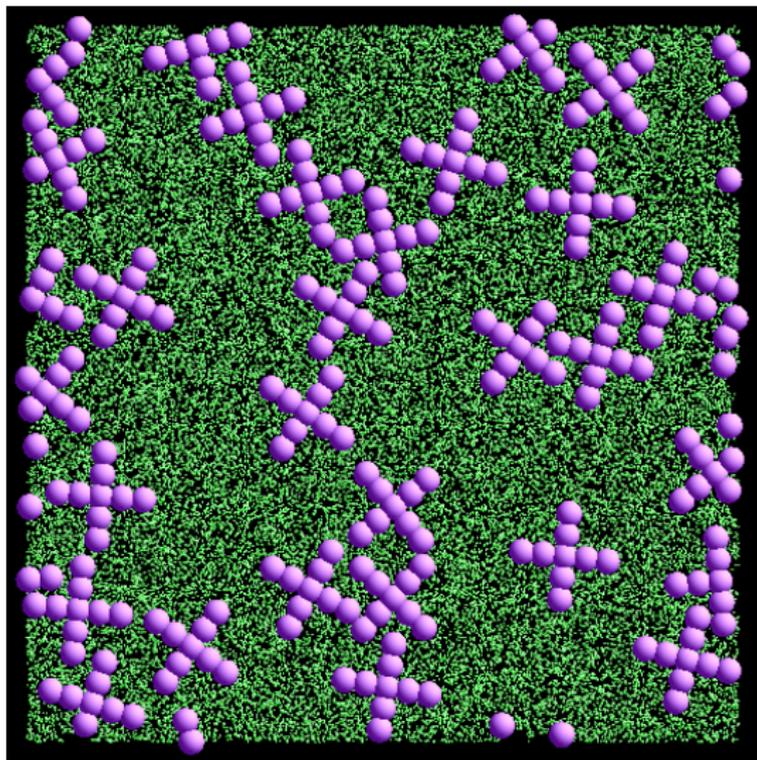
# Diffusion coefficient versus volume fraction



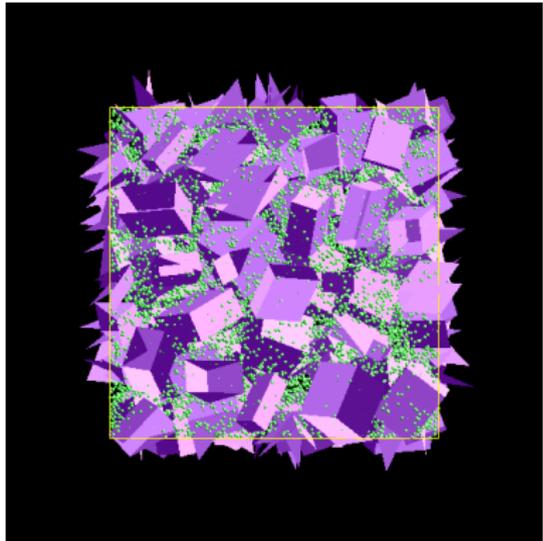
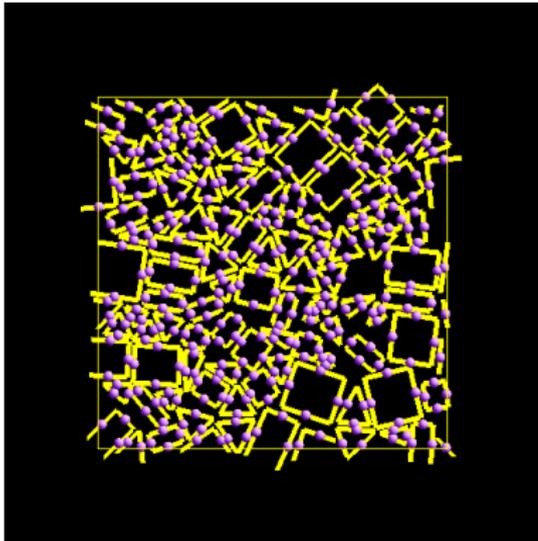
# Shear viscosity for varying shear rate and volume fraction



# Composite aspherical particles



# Generalized aspherical particles (2d and 3d)



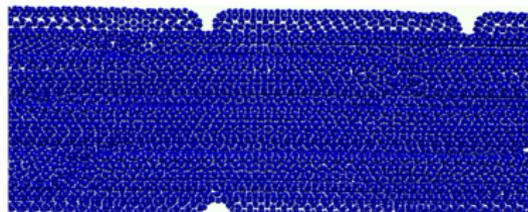
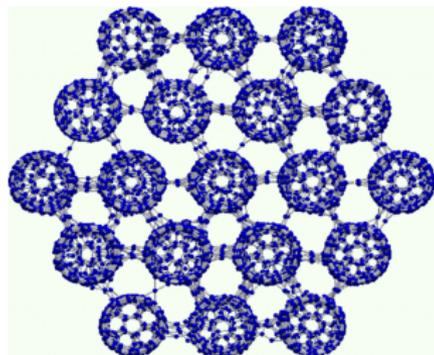
# Examples of large-scale materials modeling enabled by HPC

- **Fracture of CNT bundles** (all-atom)
- **Shock compression of low-density polymer foam** (all-atom)
- **Brain blood flow** (multi-scale)
  - coarse-grained DPD particles + Navier-Stokes fluid flow
- **Atom-to-Continuum coupling** (multi-scale)
  - all-atom + finite elements
- **Microstructural grain evolution** (mesoscale)
  - kinetic Monte Carlo, not molecular dynamics

# Fracture of CNT fibers

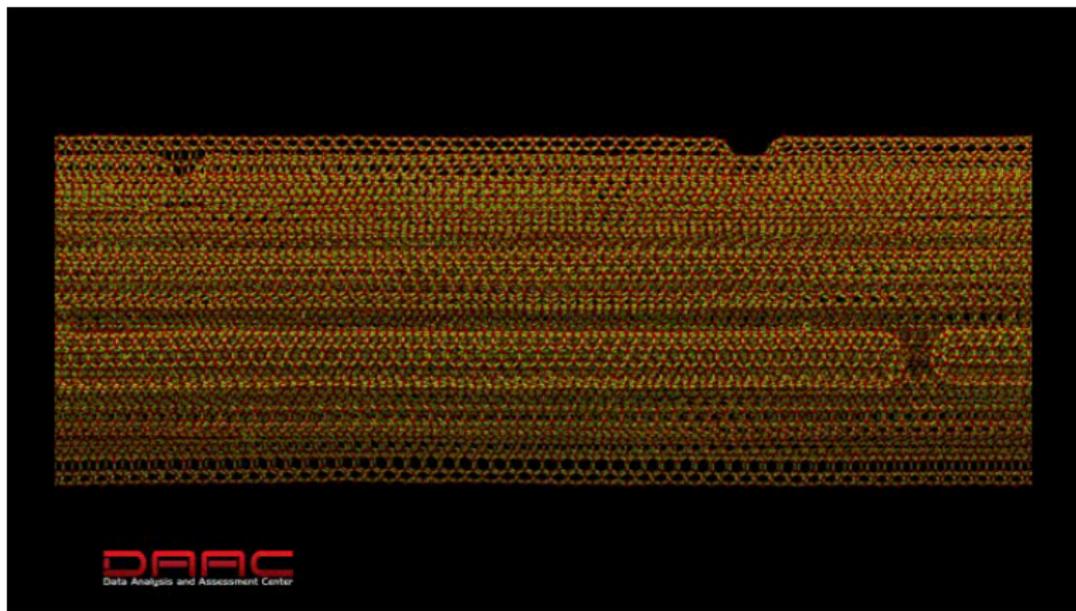
Charles Cornwell (US Army ERDC): *JCP 134, 204708 (2011)*

- Interested in **strong, light-weight materials**
- Fiber = bundle of CNTs of varying length arrayed end-to-end
- **Cross-linking** atoms and bonds added randomly



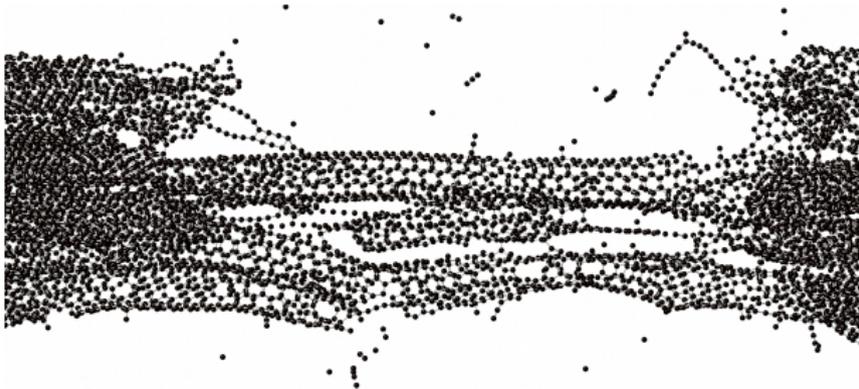
# Fracture of CNT fibers

800 nm length fiber bundle, 1.2M atoms, 6 ns simulation



# Fracture of CNT fibers

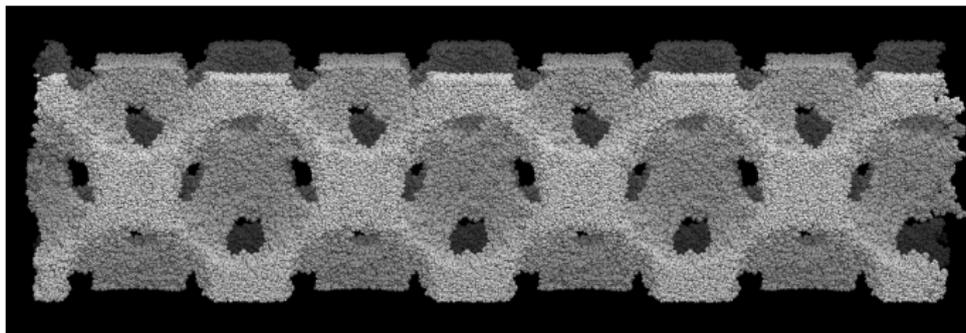
- **AIREBO** bond-order potential, tuned for C and H
- Strain applied incrementally, with relaxation in between
- **Tensile strength** at breakage increased with fiber length and cross-link density
- Maximum strength = **60 GPa** (800 nm fibers, 0.75% density)
  - high-strength steel = 2 GPa
  - Kevlar = 3.5 GPa
  - single CNT = 110 GPa



# Shock compression of low-density polymer foam

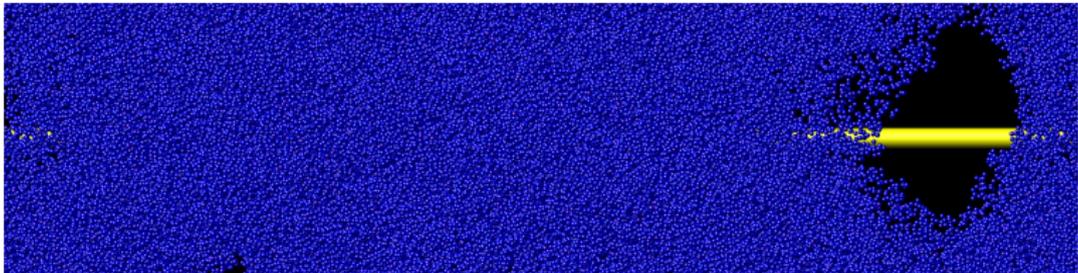
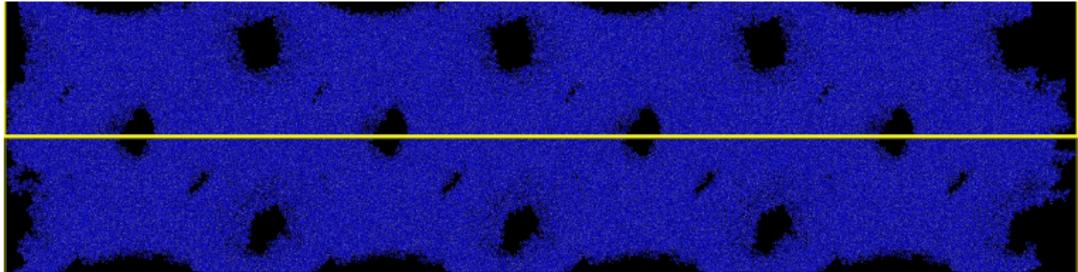
Matt Lane and Aidan Thompson (Sandia): *APS SCCM, (2011)*

- Dynamic response of **porous materials** is complex
- Foam = 50-mer chains of poly(4-methyl-1-pentene) (PMP)
- Lattice of voids  $\Rightarrow$  low density of 0.3 g/cc
- Piston strike from left at 10-30 km/sec



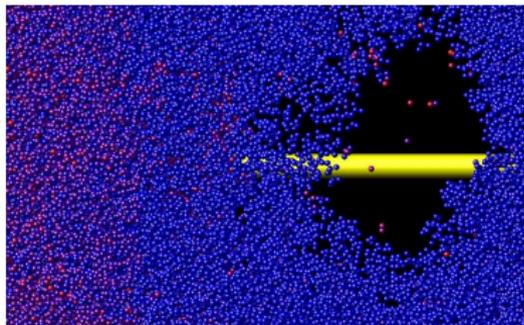
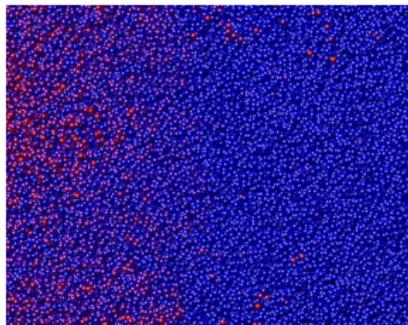
# Shock compression of low-density polymer foam

80 nm thickness sample, 1.44M atoms, tens of picoseconds



# Shock compression of low-density polymer foam

- **ReaxFF** potential to allow bond dissociation
- Requires small 0.025 fm timestep
- Observe **jetting** of polymer fragments into voids ahead of shock front
- In contrast, dense polymers exhibit little dissociation
- Quantitative capture of Hugoniot response (dense), agrees with expt

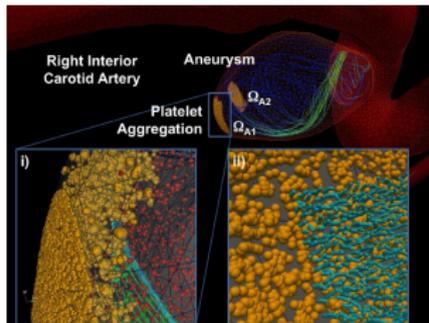
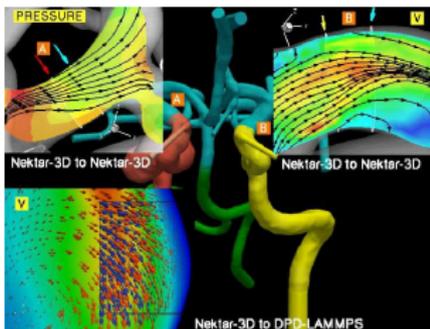


# Brain blood flow

Dmitry Fedosov (FZ Juelich) and collaborators:

*SC11 Gordon Bell competition finalist paper*

- Interested in blood flow, clot formation, **aneurysm rupture**
- Patient-specific cerebrovasculature via imaging
- **DPD particles** to resolve individual blood cells
- Continuum **Navier-Stokes** via NekTor package and spectral element solution



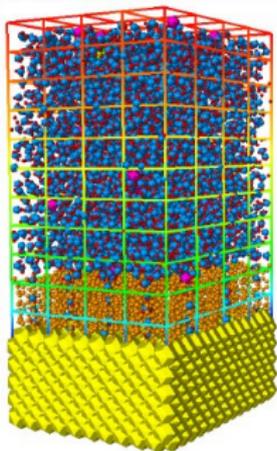
# Brain blood flow

up to 823M particles, 2B N-S unknowns, 131,072 cores of BG/P

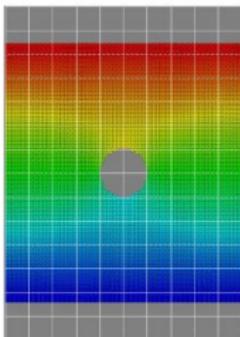


# Atom-to-Continuum coupling

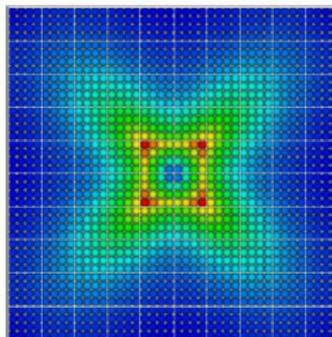
Reese Jones, Jon Zimmerman, Jeremy Templeton, Greg Wagner  
(Sandia): *CMAME* 197, 3351 (2008)



*Saltwater-electrode-CNT  
system: mesh overlaps exactly  
with water-CNT atom region*



*Circular hole in plate: mesh  
overlaps exactly with box,  
but atom region is subset*

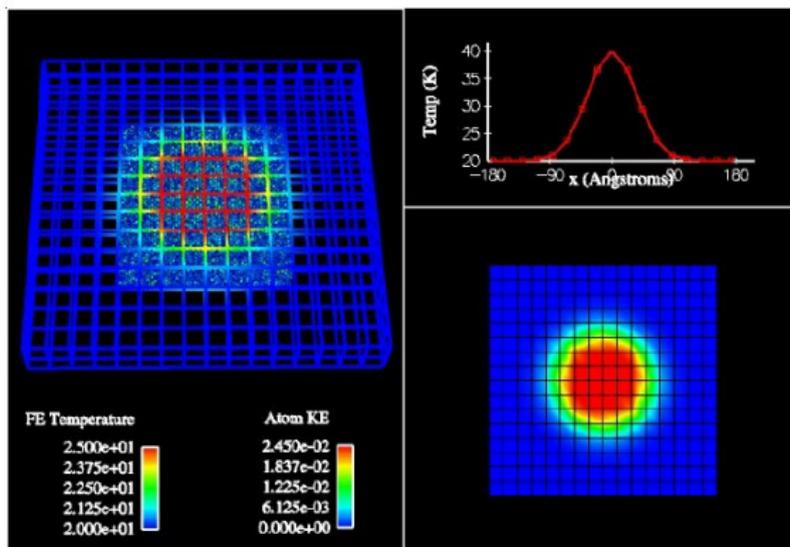


*Elastic inclusion problem:  
mesh overlaps exactly with  
box and atoms*

**Atoms** in parallel, **FE solution** in serial

# Thermal coupling with AtC package

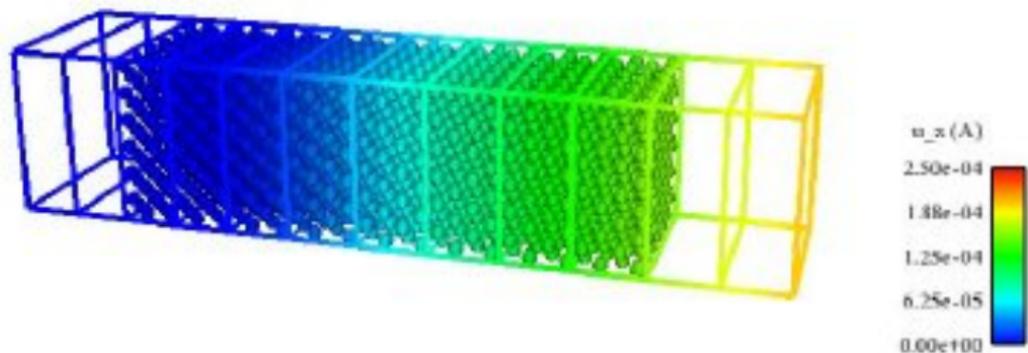
## 2D diffusion problem



- Plate with embedded MD region (~33,000 atoms)
- Initialized to temperature field with gaussian profile
- Adiabatic boundary conditions at edges



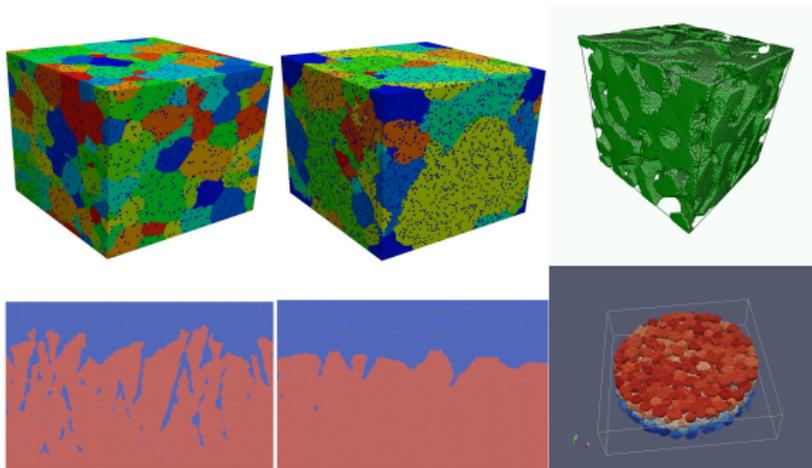
# Mechanical coupling with AtC package



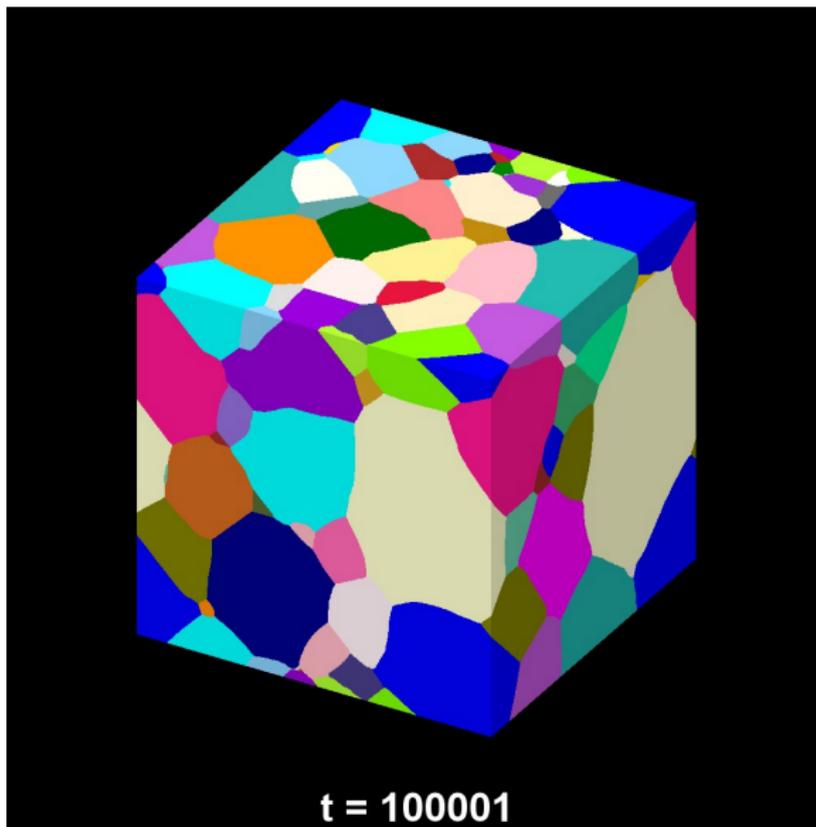
# Materials modeling via on-lattice kMC

Work with Aidan Thompson, Ed Webb, Liz Holm, Corbett Battaile (Sandia)

- Variety of models for **time evolution** of processed materials
- Length scale = atomic to mesoscale (fcc or cubic lattices)
- Time scale = **microseconds to days**
- Hamiltonian encodes physics of interest via local interactions



# Microstructural grain evolution for normal grain growth



# Summary

Exciting time to be involved in materials modeling ...

- Advances in **HPC**:
  - petaflops  $\Rightarrow$  exaflops in next few years
  - GPUs, hybrid CPU/GPU nodes
- Advances in **empirical potentials**:
  - pushing towards quantum-level accuracy
- Advances in **numerical and parallel algorithms**:
  - longer length and time scales
  - multi-scale coupling

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Progressing towards Pixar-like **ultimate goal**:  
fast & realistic modeling of any material,  
with minimum of effort by user

# Thanks

- **Funding:**

DOE and NINE funding

CRADA with Corning & 3M & BASF

- **Collaborators:**

Aidan Thompson, Flint Pierce, Jeremy Lechman, Gary Grest,  
Randy Schunk (Sandia), Pieter in't Veld (BASF)

# Thanks

- **Funding:**  
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- **Collaborators:**  
Aidan Thompson, Flint Pierce, Jeremy Lechman, Gary Grest,  
Randy Schunk (Sandia), Pieter in't Veld (BASF)
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